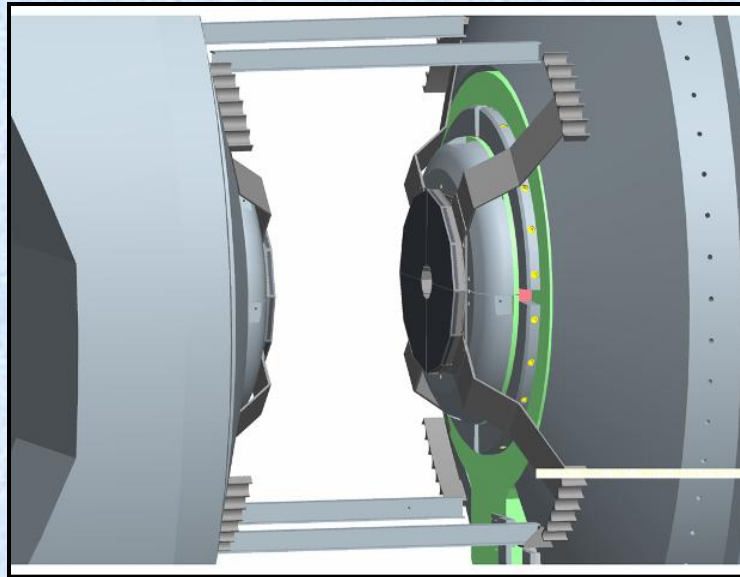


The Physics of the Reaction Plane Detector



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University of Colorado
February 6, 2007

Questions

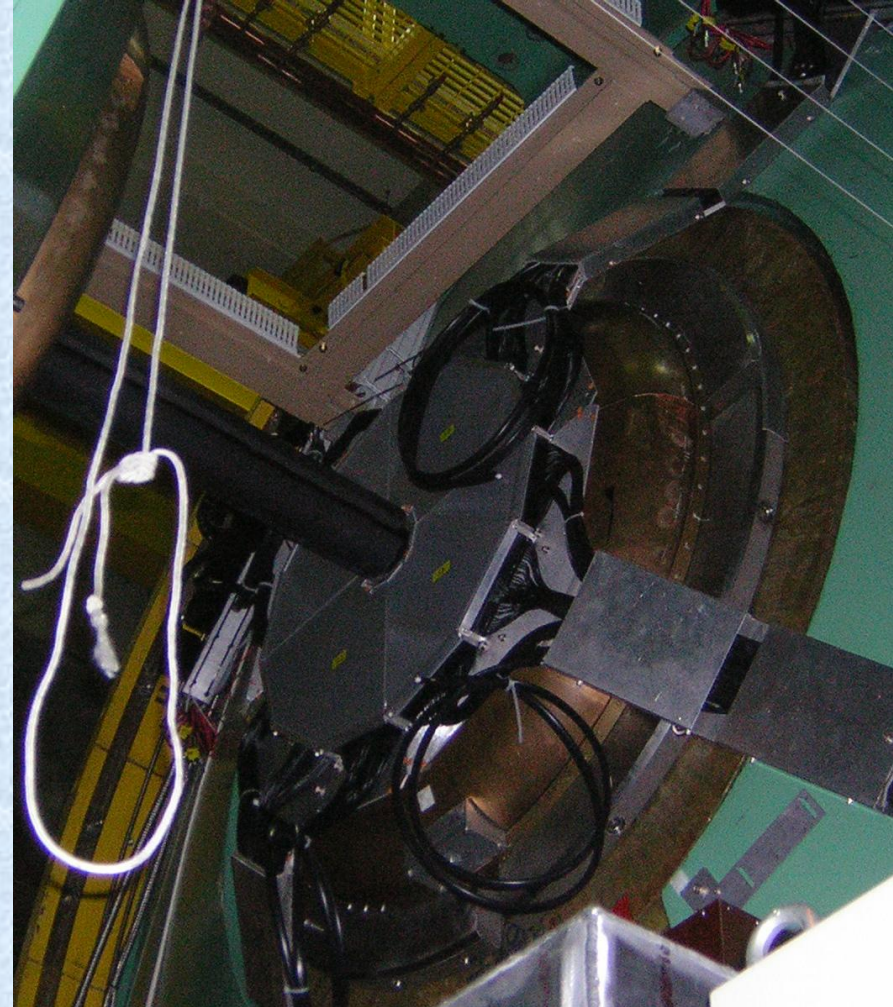
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2. How is this incorporated into physics analyses?
3. What do these measurements allow us to learn about the collision medium?

Questions

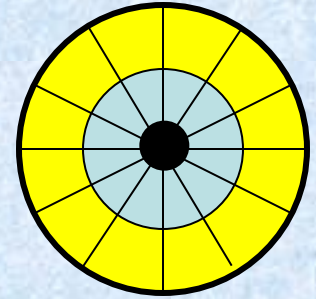
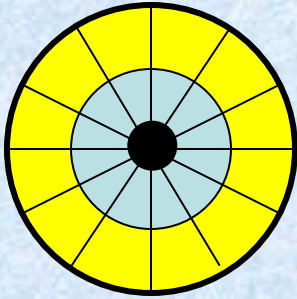
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The Reaction Plane Detector

- Review from last week:
 - Two sets of plastic scintillators positioned on either side of the collision vertex ($38 < |z| < 40\text{cm}$)
 - 12 segments in ϕ
 - 2 segments in η
 - $1.0 < |\eta| < 1.5$
 - $1.5 < |\eta| < 2.8$

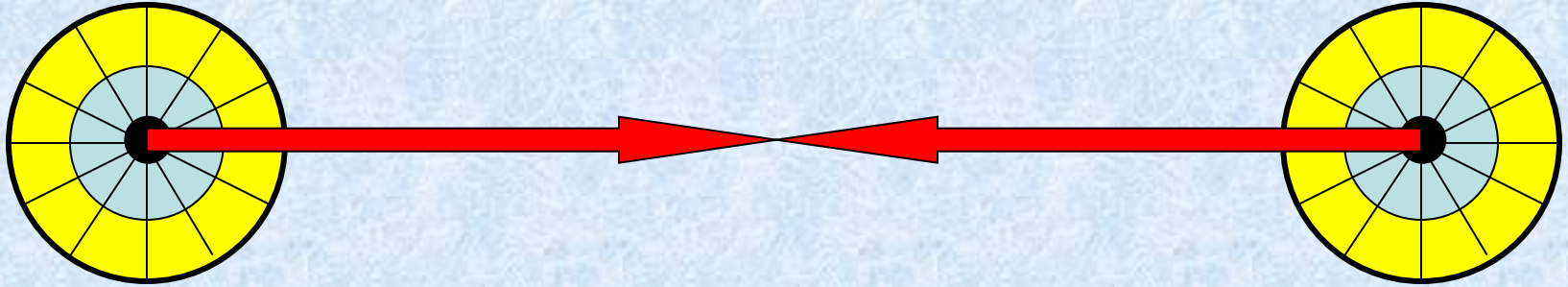


What does the reaction plane detector measure?



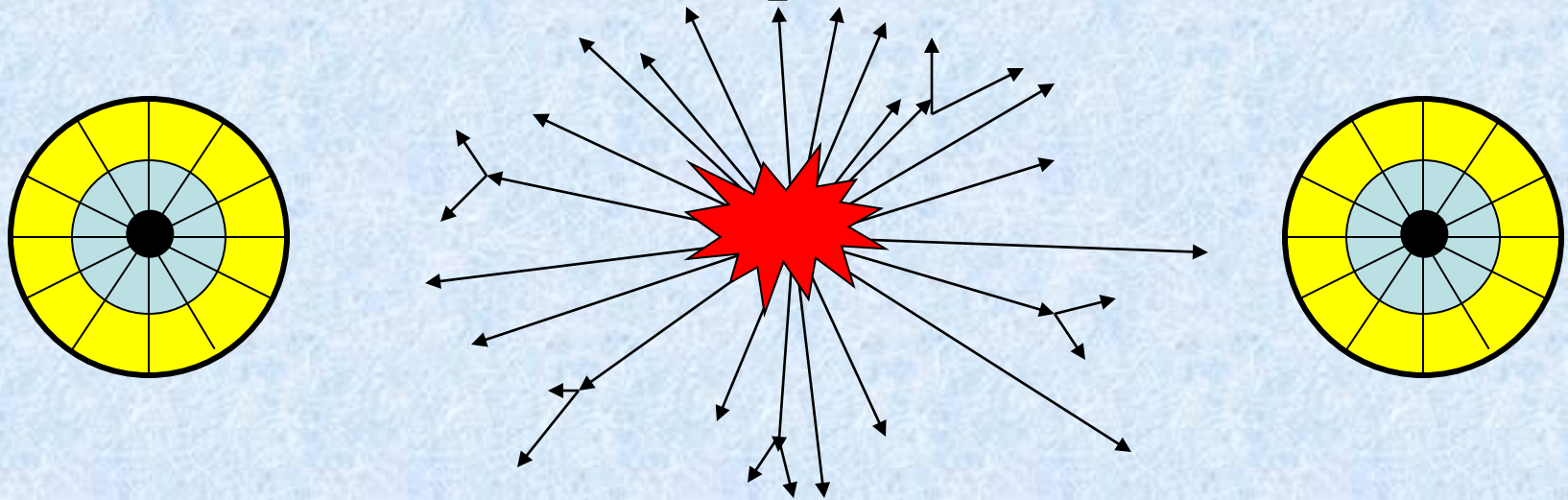
- As charged particles pass through the plastic scintillator they deposit energy and photons are produced
- These photons are collected and amplified by PMT's
- Resulting signal is proportional to the original energy deposition in each individual segment

What does the reaction plane detector measure?



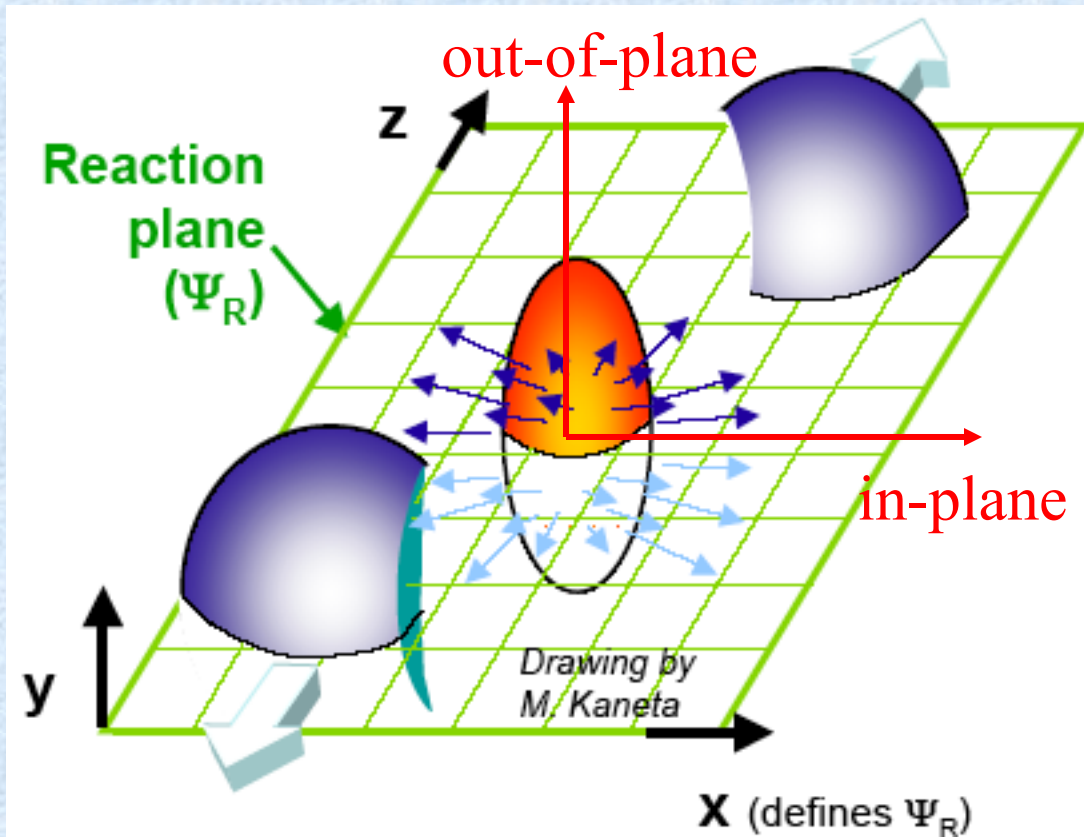
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What does the reaction plane detector measure?



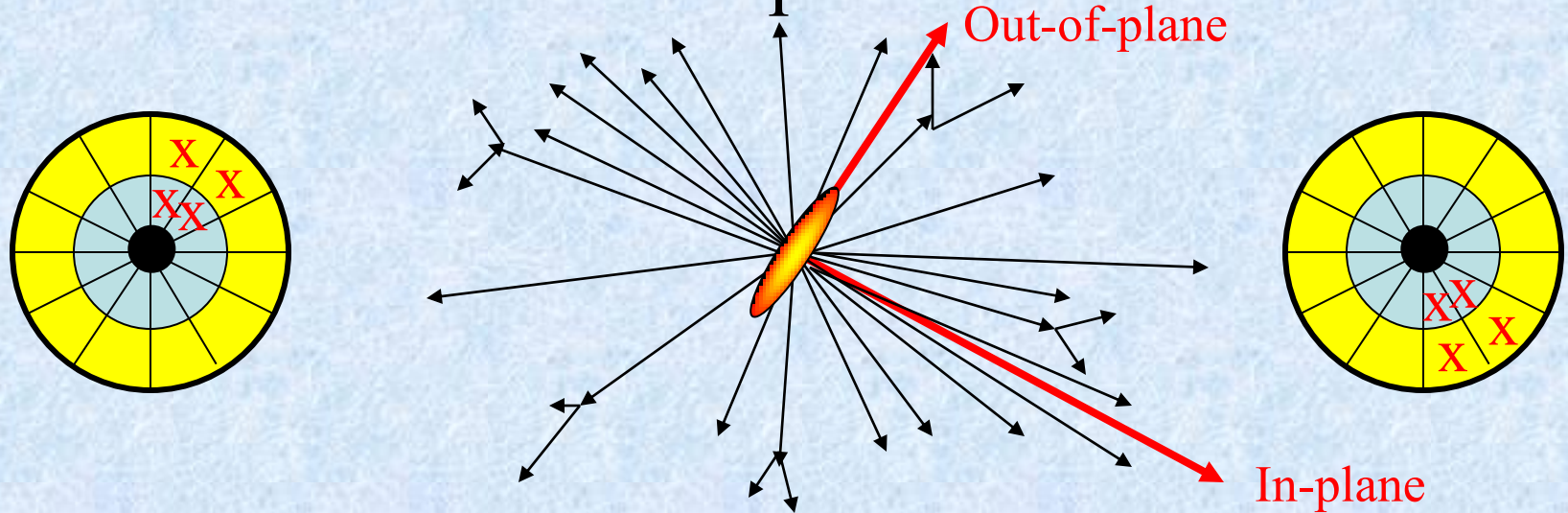
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Reaction Plane Definition



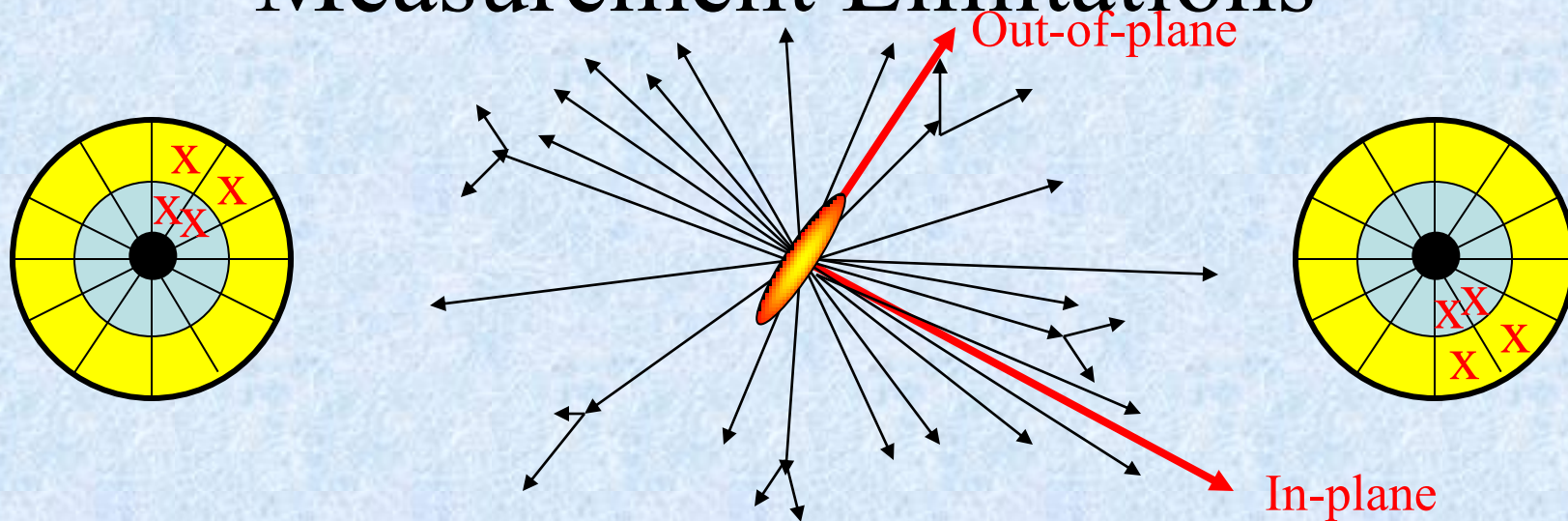
- Incomplete overlap between nuclei results in an “almond” shaped collision region
- Characterize collision region by reaction plane (defined by beam direction and vector between centers of colliding nuclei)
- Pressure gradient to expand is greatest along short axis (in-plane)
- Results in greater particle emission in-plane

What does the reaction plane detector measure?



- In non-central collisions the difference between the in-plane and out-of-plane pressure gradients results in preferential in-plane particle emission
- This shows up in the reaction plane detector as an increased energy deposition in those segments aligned with the reaction plane
- Allows for an event-by-event determination of Ψ_R

Measurement Limitations



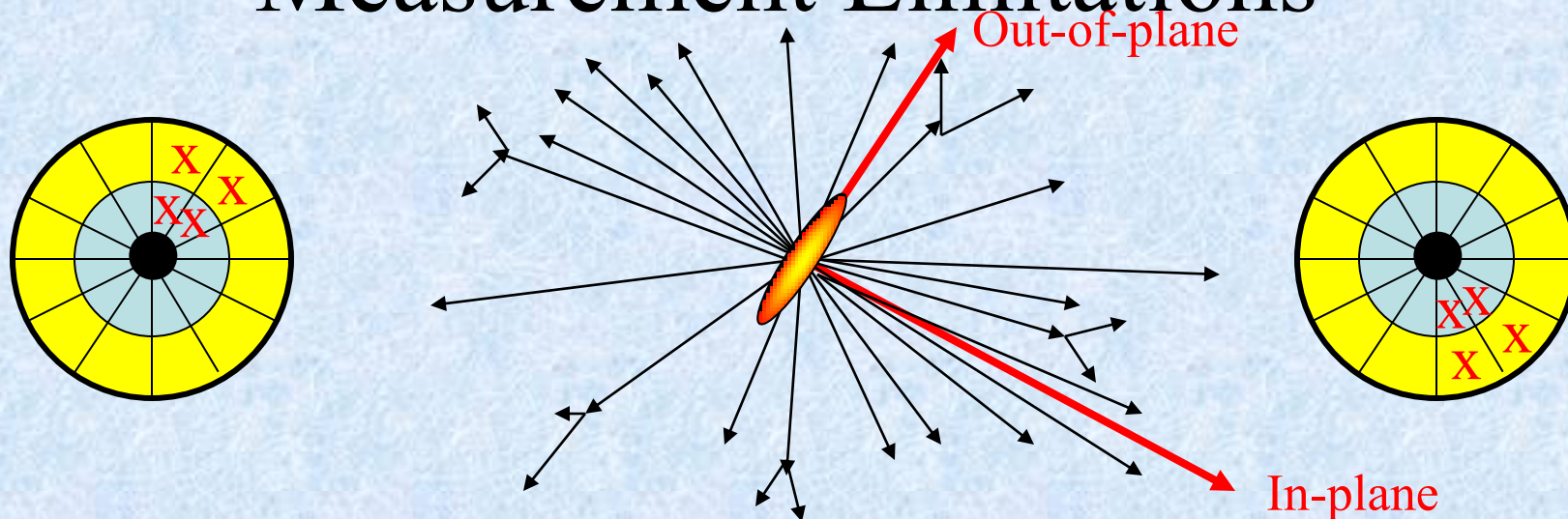
1. Back to back jets:

- Create a spray of particles at 180°
- Could mask or bias preferential angle of emission by pressure gradients
- Preferentially generated in mid-rapidity region \therefore would only influence Ψ_R determination in outer scintillator segments

2. Collision centrality

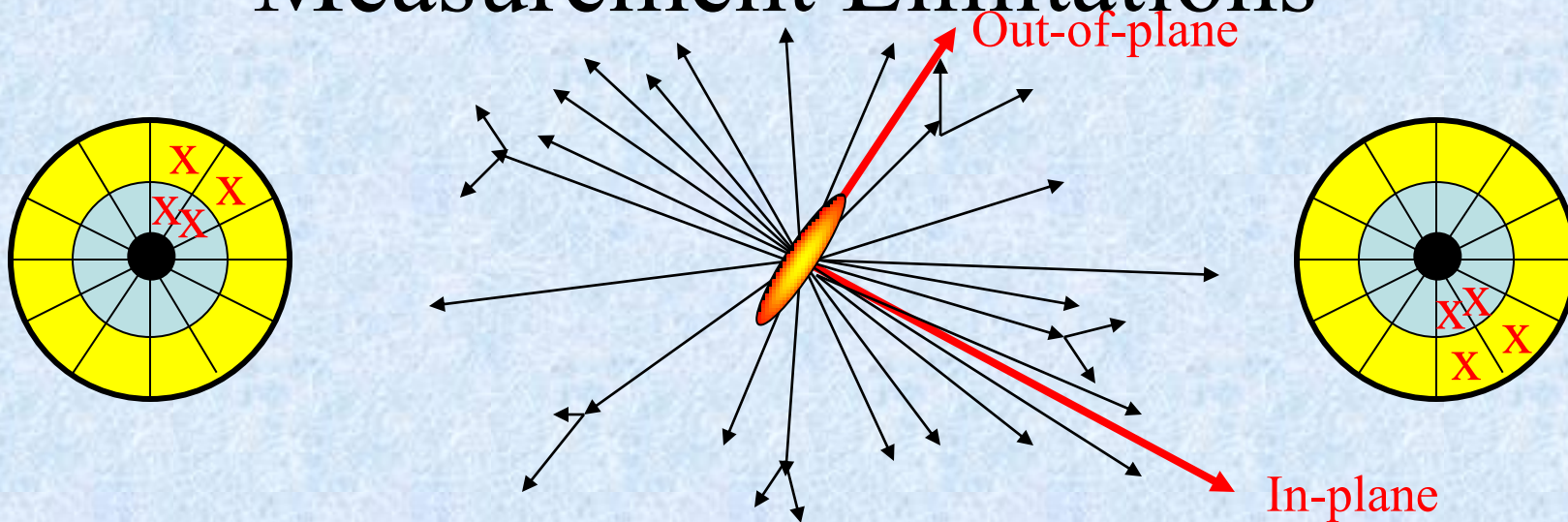
3. Reaction plane resolution

Measurement Limitations



1. Back to back jets:
2. Collision centrality:
 - The more central the collision the more spherical the overlap region and weaker the difference in the pressure gradients
 - Hence ability to determine Ψ_R is highly dependent on the collision centrality
3. Reaction plane resolution

Measurement Limitations



1. Back to back jets:
2. Collision centrality:
3. Reaction plane resolution:
 - Correction factor that is applied to account for the fact that the finite number of particles used to determine the reaction plane result in a limited resolution in the angle of the measured reaction plane

Reaction Plane Resolution

- Method 1: Direct Calculation

$$\sigma_{RP} = \left\langle \cos \left[n \left(\psi_{\text{expt}} - \Psi_{\text{true}} \right) \right] \right\rangle$$

A priori
not known

Reaction Plane Resolution

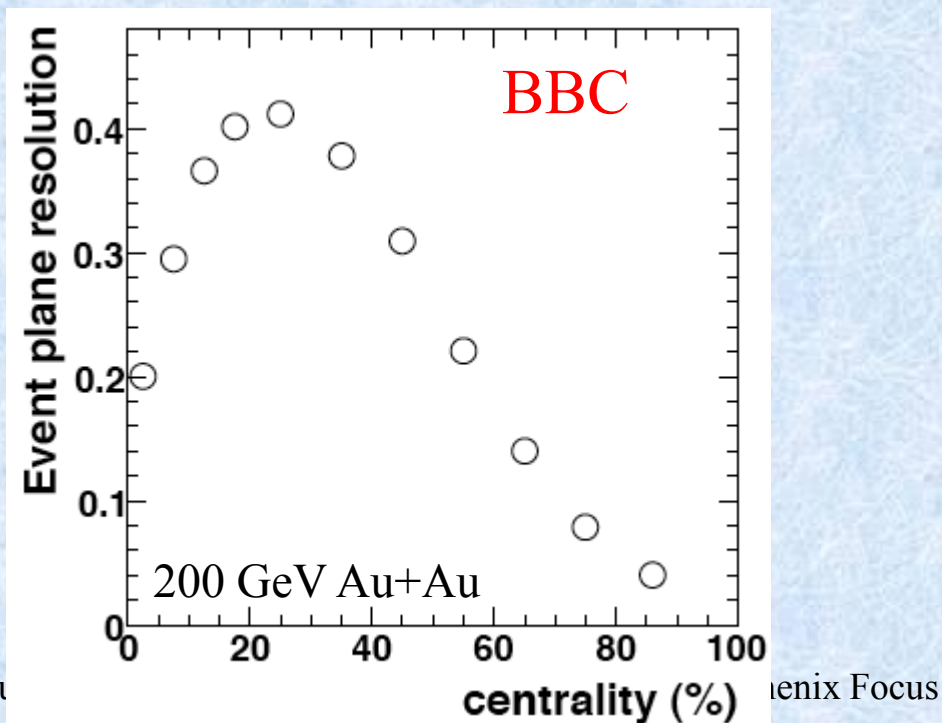
- Method 2: Sub-event method
 - Use two independent sets of particles (a,b) from the same event to calculate the reaction plane
 - Compare reaction plane from each sub-event to determine resolution

$$\sigma_{RP} = \sqrt{\left\langle \cos \left[n \left(\psi_n^a - \psi_n^b \right) \right] \right\rangle}$$

- Requires assumptions:
 - Both sub-events contain the same number of particles
 - Degree of flow is the same in each sub-event
 - Any particle correlations other than flow are negligible

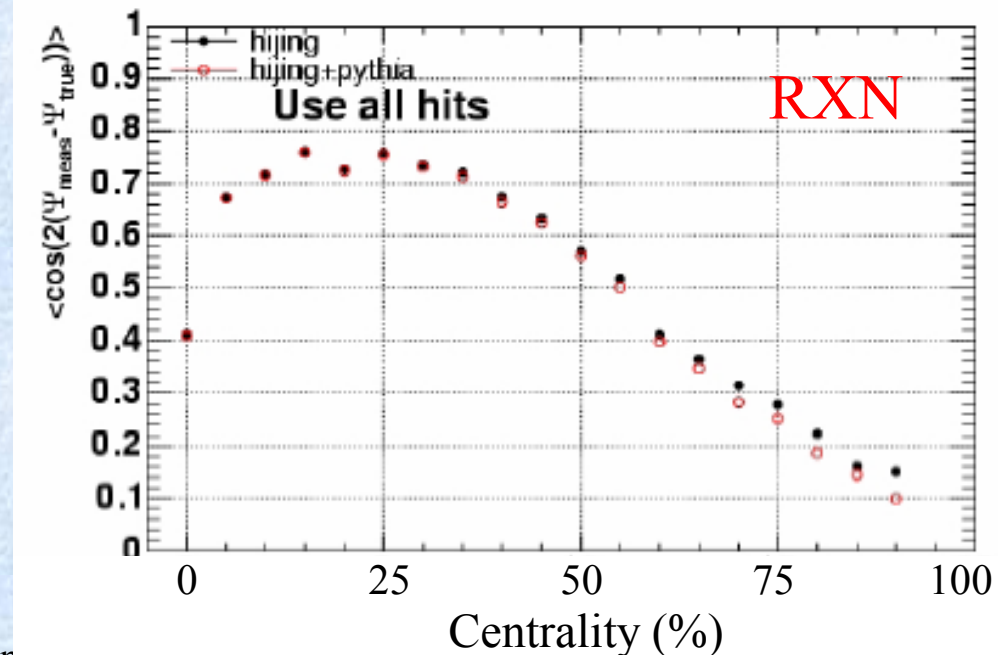
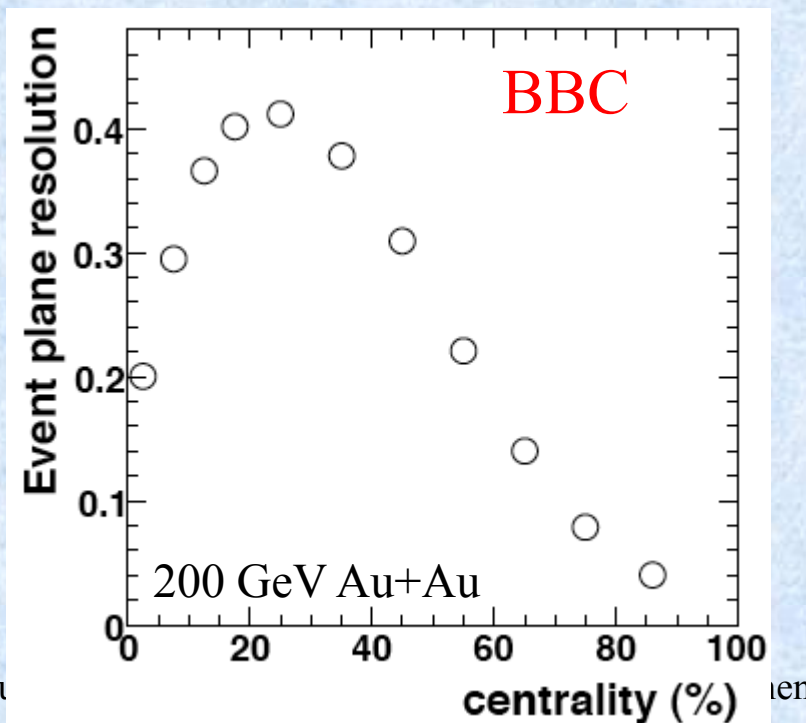
Reaction Plane Resolution

- Method 2: Sub-event method application
 - Each set of BBC's compose a single sub-event
 - BBC's are symmetric in acceptance so it is reasonable to assume both sub-events contain the same number of particles and degree of flow
 - BBC's are far forward in rapidity thus any particle correlations other than flow are negligible ($3.1 < |\eta| < 3.9$)



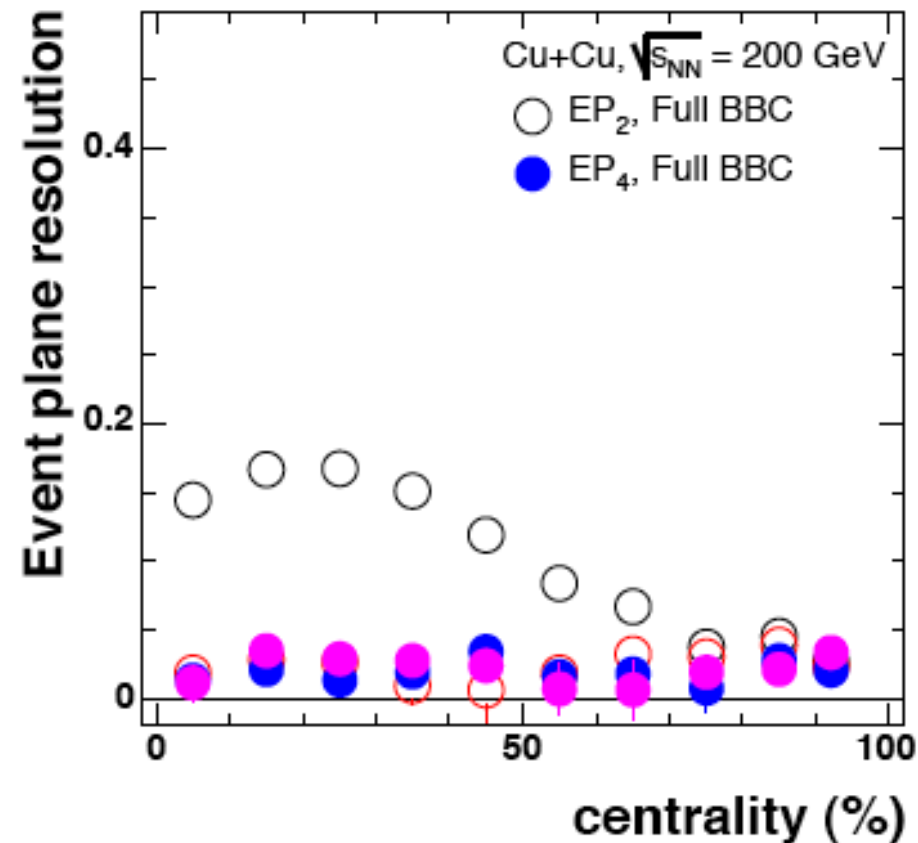
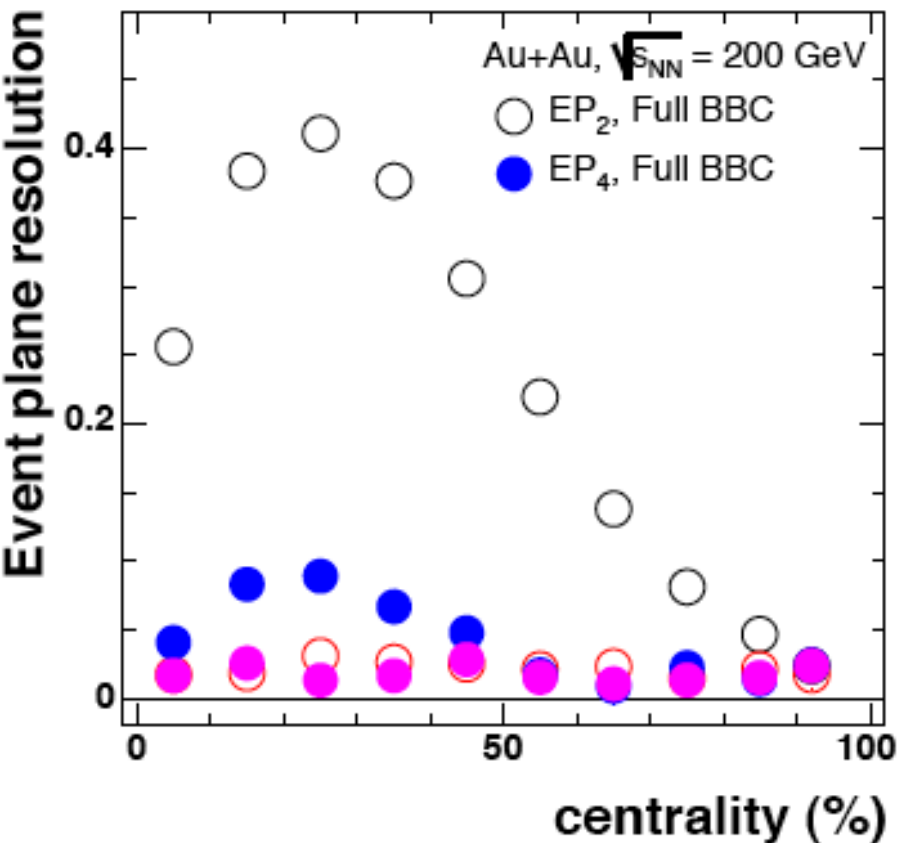
Reaction Plane Resolution

- Method 2: Sub-event method application
 - Same technique can be applied using the reaction plane detector
 - Rapidity coverage is greater $1.0 < |\eta| < 2.8$ compared to $3.1 < |\eta| < 3.9$ of BBC's
 - Incident multiplicity is greater
 - Pb converter enhances signal by converting neutrals to charged particles that can be detected in the scintillators



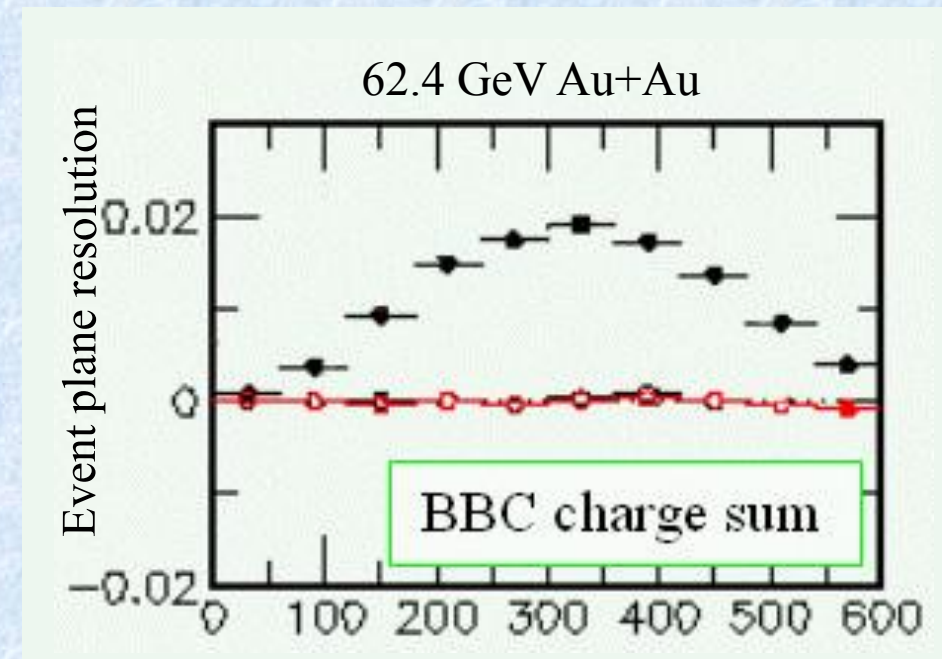
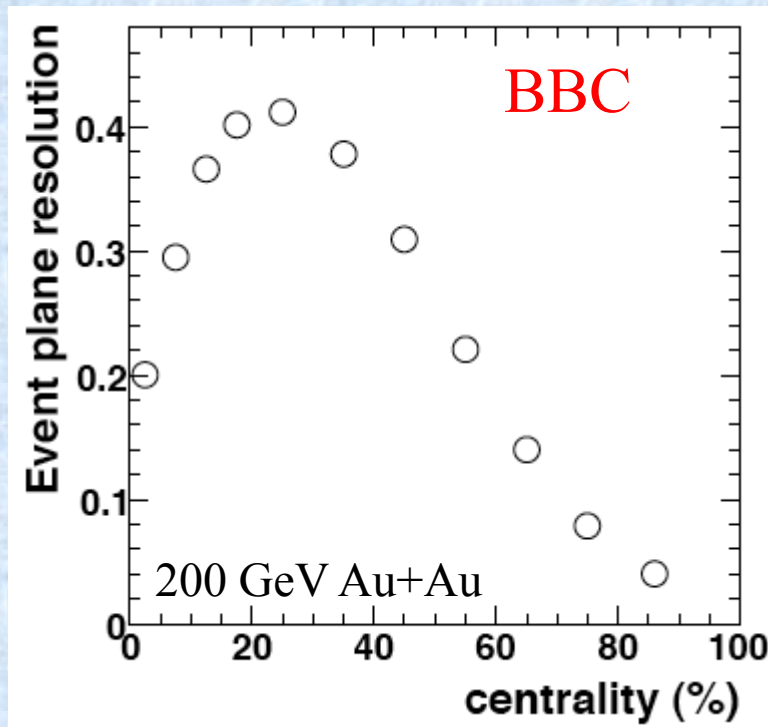
Reaction Plane Resolution

- Ability to determine reaction plane is dependent upon BBC incident multiplicity
- Beams of light ions and low energies result in fewer particles
- Future measurements of v_2 in these systems will require an improved reaction plane resolution



Reaction Plane Resolution

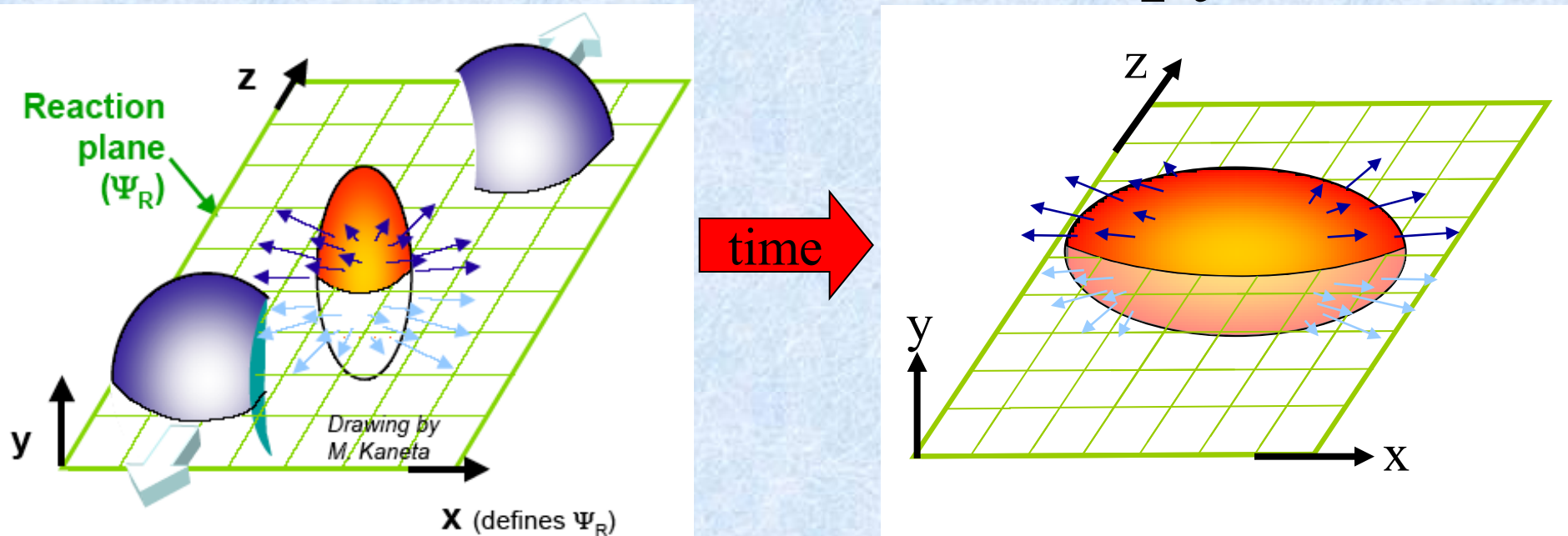
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Questions

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Azimuthal Anisotropy



1. Collision Feature \Rightarrow degree of overlap in colliding nuclei
2. Scattering converts spatial anisotropy to momentum anisotropy
3. Measurable Quantity \Rightarrow momentum anisotropy of produced particles

$$\frac{dN}{d(\psi - \Psi_{true})} \propto 1 + 2v_1 \cos(\varphi - \Psi_R) + 2v_2 \cos(2(\varphi - \Psi_R)) + \dots$$

↑
↑

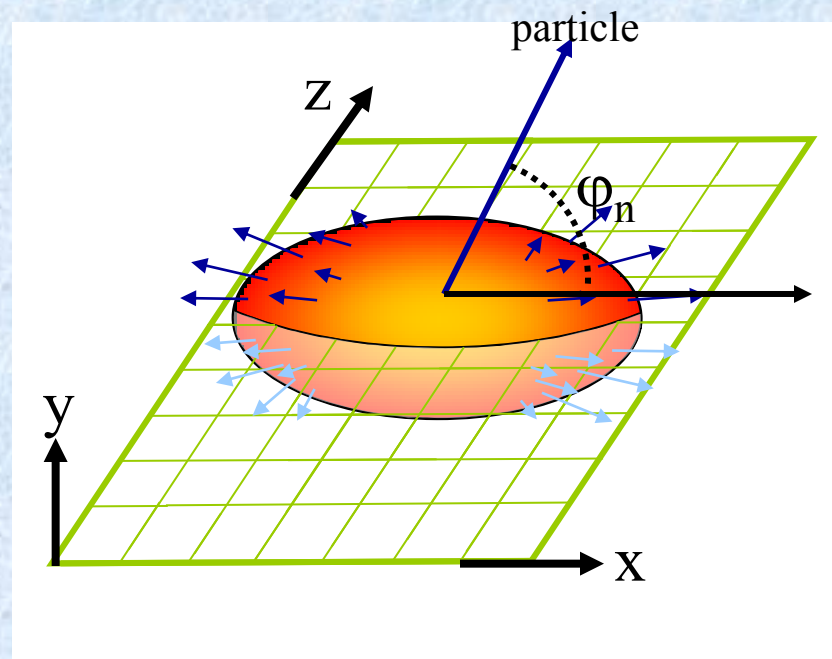
Directed Flow
Elliptic Flow

Measuring Elliptic Flow

- Elliptic Flow:
 - Second harmonic coefficient of the Fourier expansion of the azimuthal distribution of particles
 - $v_2 = \langle \cos(2\varphi_n) \rangle$.
- For each collision event determine reaction plane
- Measure angular distribution of emitted particles wrt reaction plane, φ_n
- Calculate v_2 per event
- Examine dependence on centrality, momentum, particle id, rapidity, collision energy, collision species....

$$v_2^{meas} = \langle \cos(2\varphi) \rangle$$

φ = angle of each particle
wrt reaction plane



Reaction Plane Resolution

$$v_2^{true} = \frac{\langle \cos[2(\varphi)] \rangle}{\sigma_{RP}} \quad \rightarrow \quad v_2^{true} = \frac{\langle \cos[2(\varphi)] \rangle}{\sqrt{\langle \cos[2(\psi_2^a - \psi_2^b)] \rangle}}$$

- Resolution must be applied as a correction factor to any experimental measurement of flow
- Always results in $v_2^{true} > v_2^{meas}$
- The precision to which the reaction plane can be determined directly limits any measurement of flow and translates into the statistical error

Error Analysis

$$\delta(v_2^{\text{expt}}) \approx \frac{1}{\sqrt{N_{\text{signal}}}}$$
$$\delta(v_2^{\text{true}}) = \frac{\delta(v_2^{\text{expt}})}{\sigma_{RP}} \approx \frac{1}{\sigma_{RP} \sqrt{N_{\text{signal}}}}$$

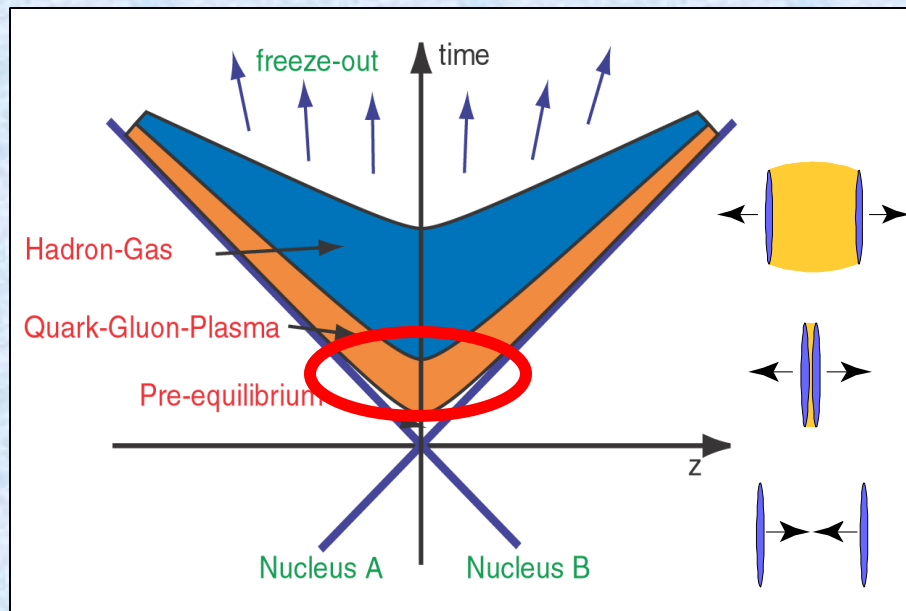
- The two key components of the statistical error in any elliptic flow measurements are the signal strength and the reaction plane resolution
- Statistical power of measured v_2 is reduced by $(\sigma_{RP})^2$
- Improvement provided by reaction plane detector compared to BBC's:

$$\left(\frac{\sigma_{RP}^{RXN}}{\sigma_{RP}^{BBC}} \right)^2 = \left(\frac{0.40}{0.70} \right)^2 \approx 3$$

Questions

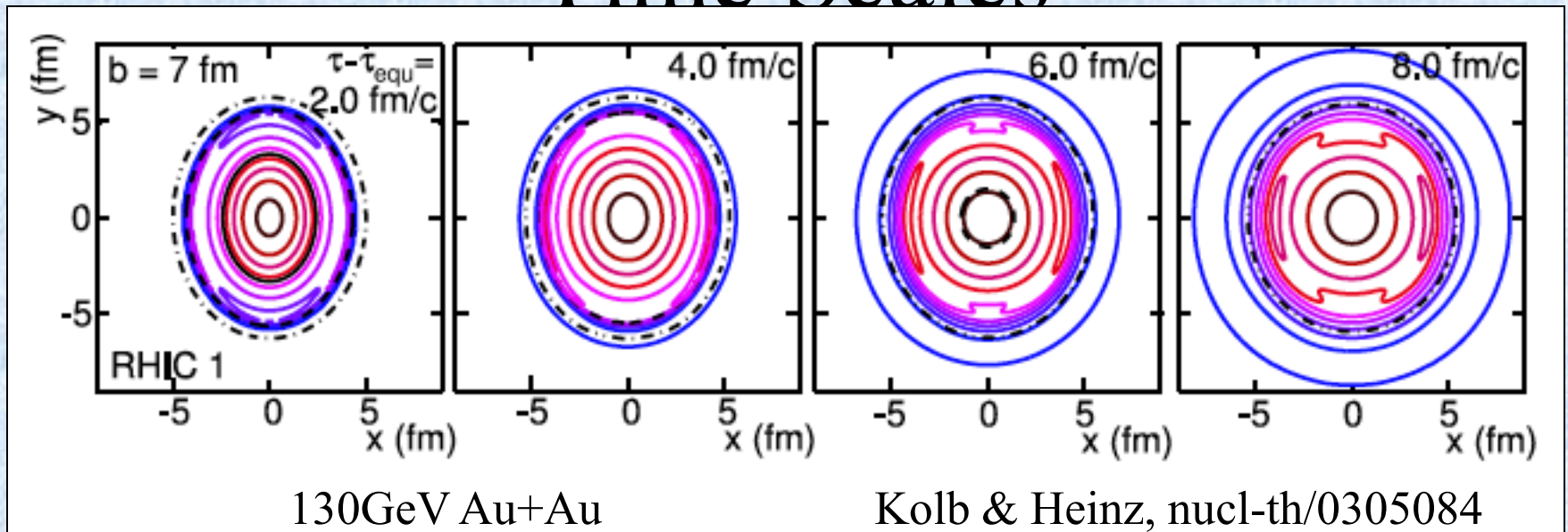
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Collision Evolution



- Elliptic flow studies probe the early stages of the collision when the initial collision geometry still dominates
- System can be described by thermodynamic quantities only if thermal equilibrium is achieved
- This occurs during a heavy ion collision when the energy deposited during the collision generates large numbers of particles that interact & rescatter among themselves

Time Scales

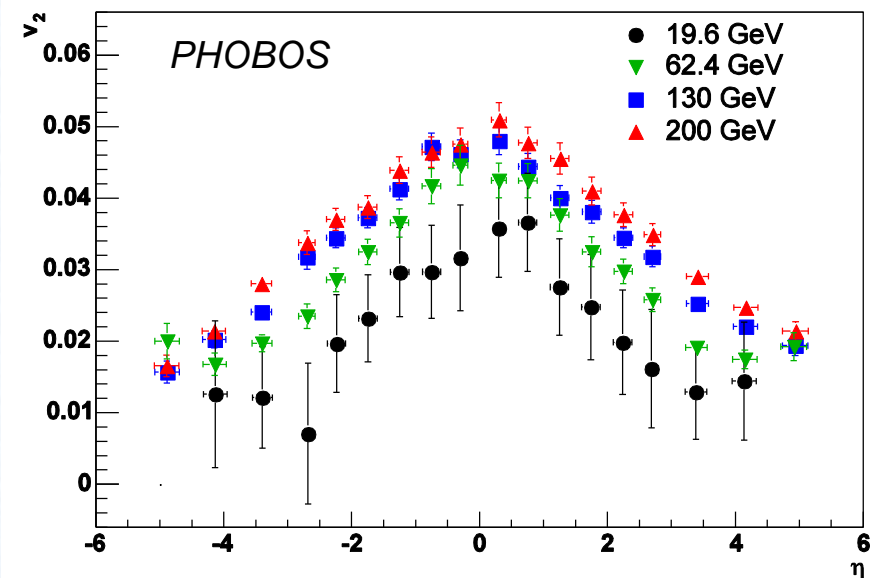


- Hydrodynamical models are used to calculate the time evolution of the energy density in-plane
- If thermal equilibrium is achieved:
 - late then asymmetry will be small
 - early then asymmetry will be large
- Experimental observation of v_2 implies local thermal equilibrium achieved while spatial anisotropy exists (ie short time scale)

Early Elliptic Flow Results

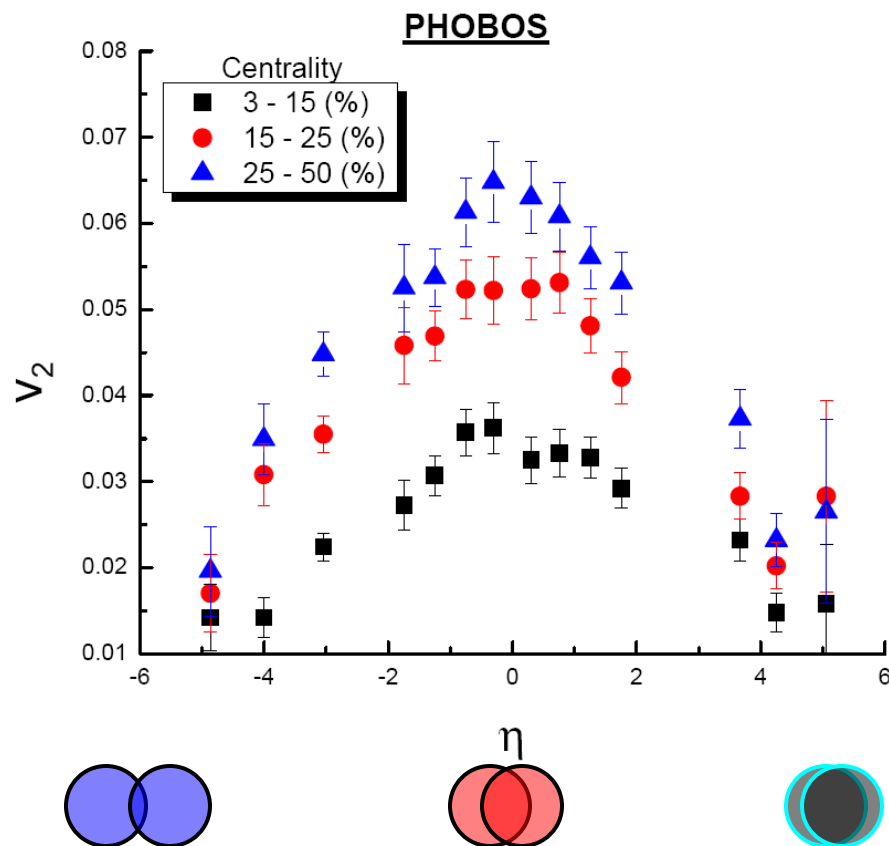
Centrality:

As % centrality decreases overlap region becomes less asymmetric \therefore less difference in pressure gradient

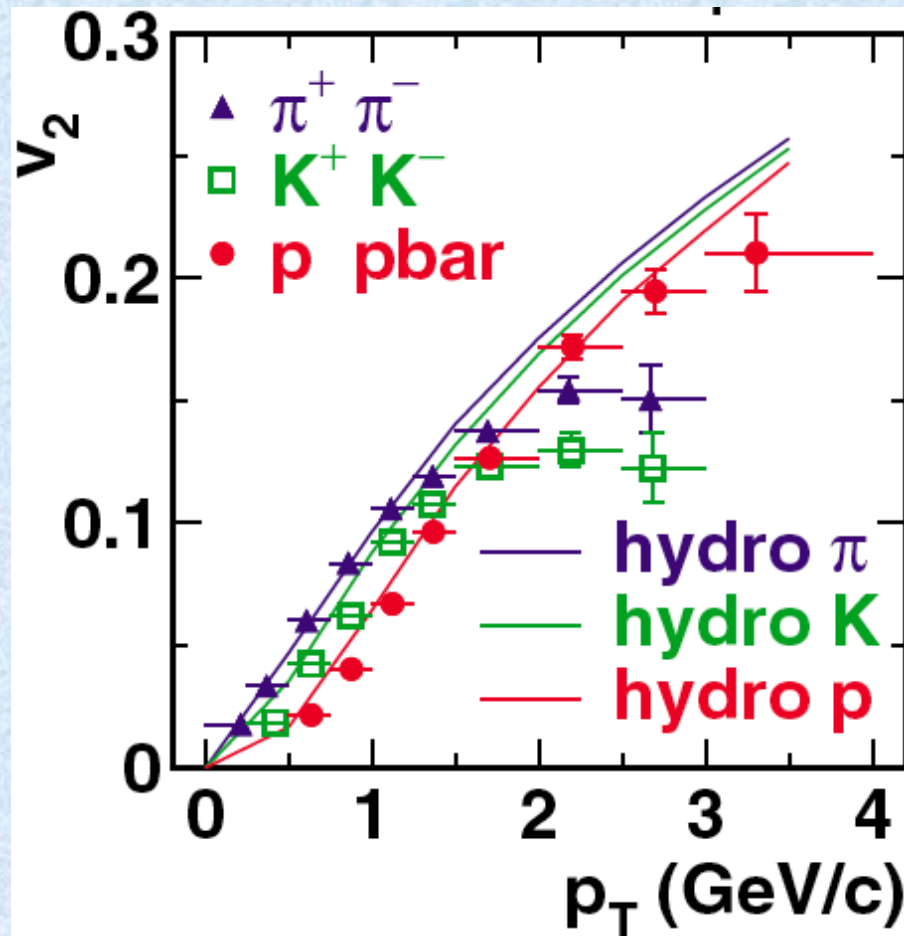


Collision Energy:

As collision energy decreases energy density pressure gradient also decreases resulting in decreased flow



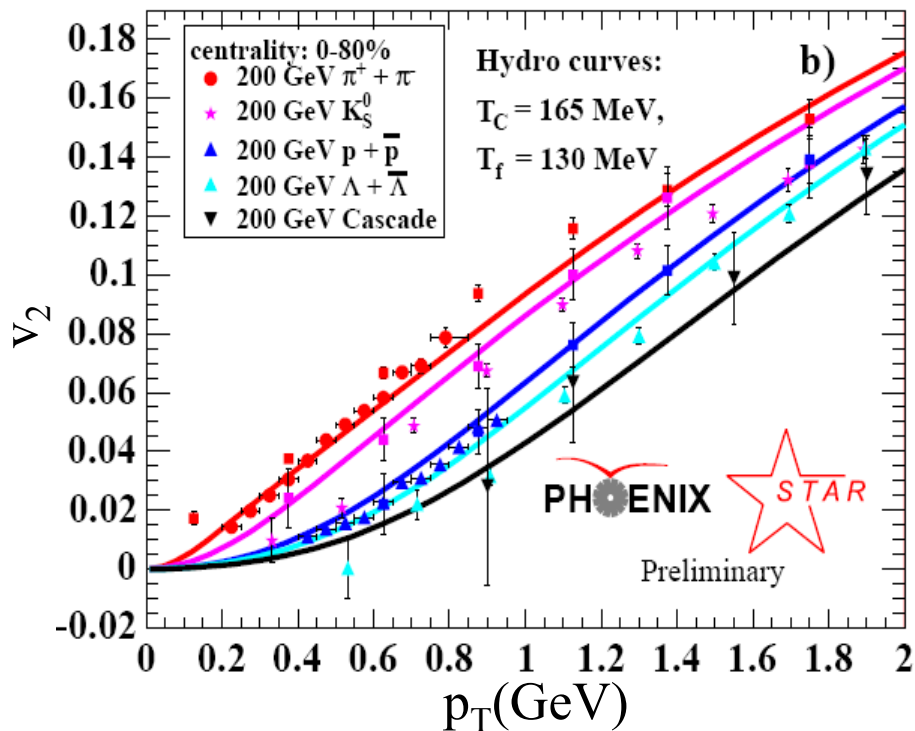
Early Elliptic Flow Results



White Paper Conclusions:

- Identified hadron v_2 is well reproduced by hydro calculations at low p_T
- Magnitude of v_2 requires thermal equilibration time of $\sim 0.6\text{-}1.0$ fm/c

Hydrodynamics Lessons



✓ Thermal Equilibration:

Large elliptic flow signal implies fast equilibration time of collision system, $t \sim 1$ fm/c.

x Weakly interacting QGP:

Classic concept of a quark gluon plasma as an ideal relativistic gas with color deconfinement.

✓ Strongly interacting non-hadronic medium:

Fluid-like properties of collision medium indicate significant interactions occur among the particles.

Press Release: “Perfect Liquid”

Contact: Karen McNulty Walsh, (631) 344-8350 or Mona S. Rowe, (631) 344-5056

 [Print-friendly](#)  [E-mail Article](#)

RHIC Scientists Serve Up “Perfect” Liquid

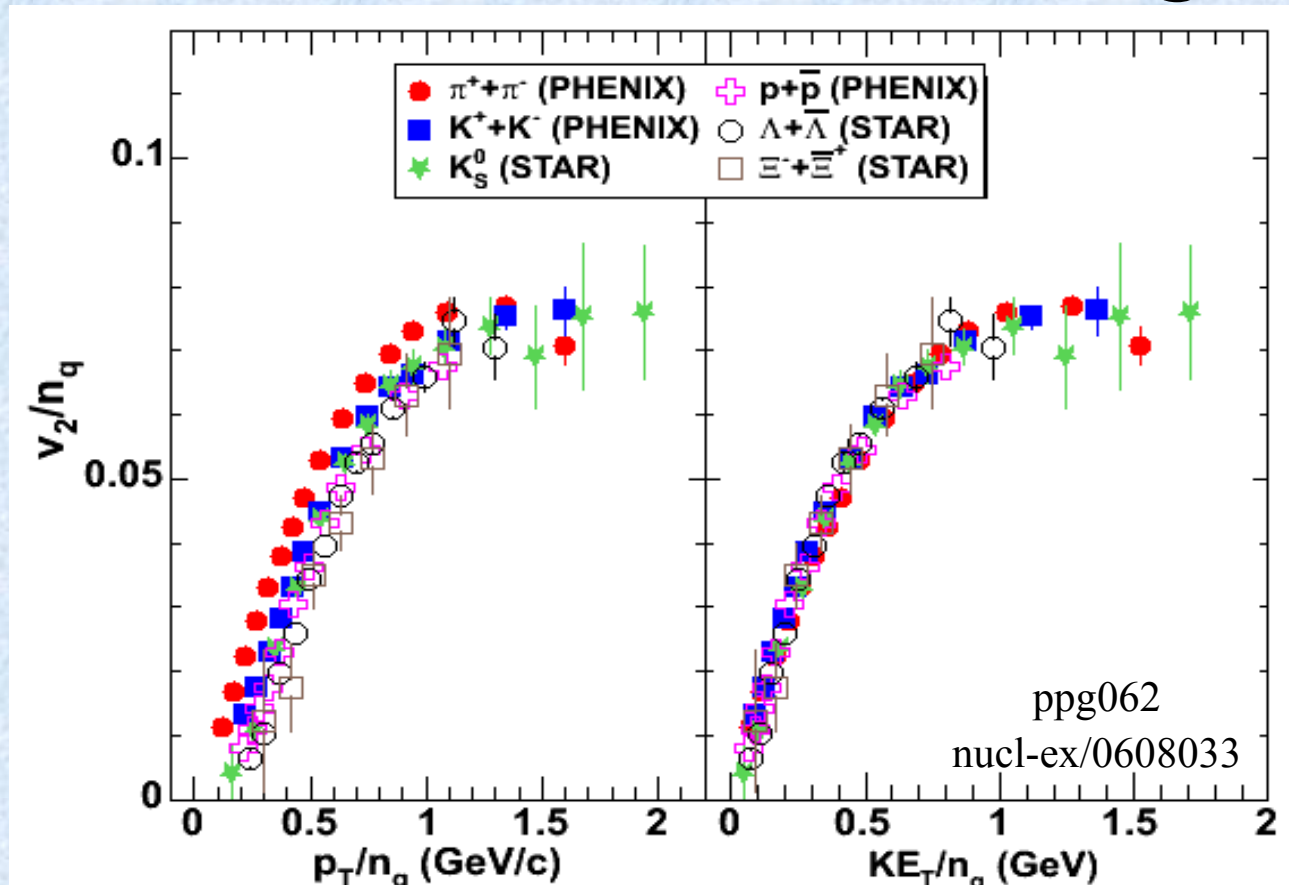
New state of matter more remarkable than predicted -- raising many new questions

April 18, 2005

TAMPA, FL -- The four detector groups conducting research at the [Relativistic Heavy Ion Collider](#) (RHIC) -- a giant atom “smasher” located at the U.S. Department of Energy’s Brookhaven National Laboratory -- say they’ve created a new state of hot, dense matter out of the quarks and gluons that are the basic particles of atomic nuclei, but it is a state quite different and even more remarkable than had been predicted. In [peer-reviewed papers](#) summarizing the first three years of RHIC findings, the scientists say that instead of behaving like a gas of free quarks and gluons, as was expected, the matter created in RHIC’s heavy ion collisions appears to be more like a *liquid*.

- **What is a “Perfect Liquid”?**
 - Liquid = a substance that exhibits a readiness to flow with little or no tendency to disperse, and relatively high incompressibility.
 - Perfect Liquid = liquid that exhibits no resistance to flow
- **How does this apply to RHIC?**
 - Strong elliptic flow observed that is well described by hydrodynamic models
 - Magnitude, particle type up to $p_T \sim 1 - 2 \text{ GeV}/c$
 - Fast thermalization ($\tau < 1 \text{ fm}/c$)
 - Little or no viscosity

Quark Number Scaling



- Indicates quark-like degrees of freedom in flowing matter for hadrons made of light quarks
- Recombination consistent with observed n_q scaling of v_2

Remaining Questions

- Elliptic flow measurements have been successful at revealing the nature of the collision medium BUT many more measurements remain
 - Heavy quarks:
 - Do they couple to the medium?
 - Quarkonia:
 - Test of regeneration models
 - High p_T π^0 's:
 - Parton energy loss as a function of path length in the medium
 - Intermediate p_T direct photons:
 - Test predictions of jet-medium interaction as a function of path length in the medium
- Statistics, Statistics, Statistics.....

Do heavy quarks flow?

Non-photonic Electrons:

Semi-leptonic charm & bottom decays } Signal

Di-electron decays of ρ , ω , ϕ , J/ψ

Kaon decay

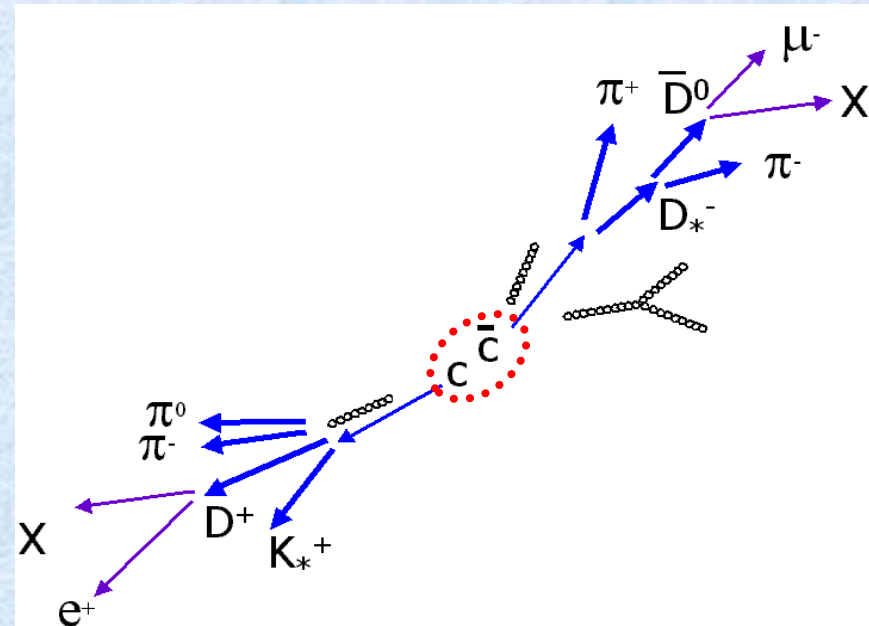
Photonic Electrons:

Dalitz decays of π^0 , η , η' , ω , ϕ

Photon conversions

Direct photon (negligible)

Back
ground



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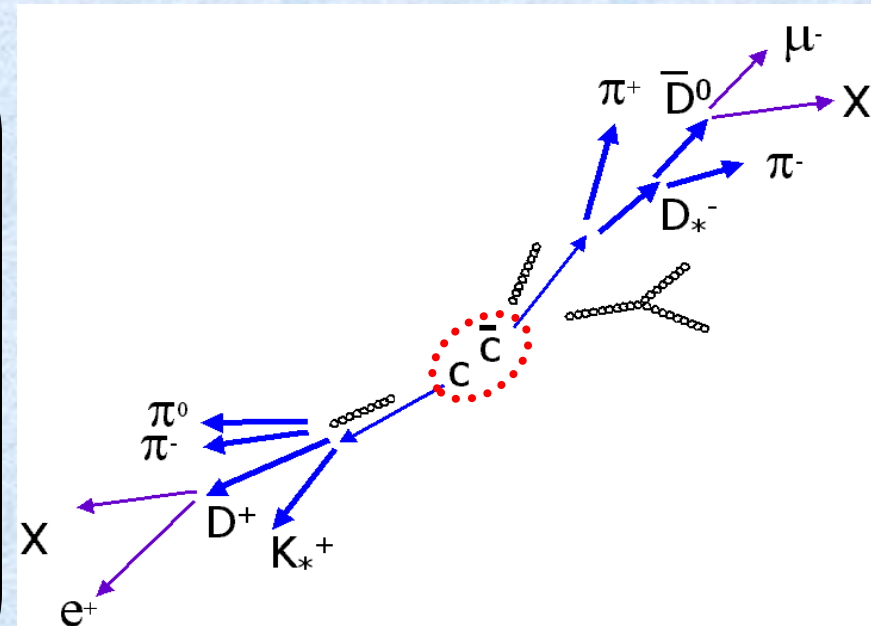
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Heavy flavor electron v_2 :

Is the single electron v_2 representative
of the v_2 of the parent heavy meson?

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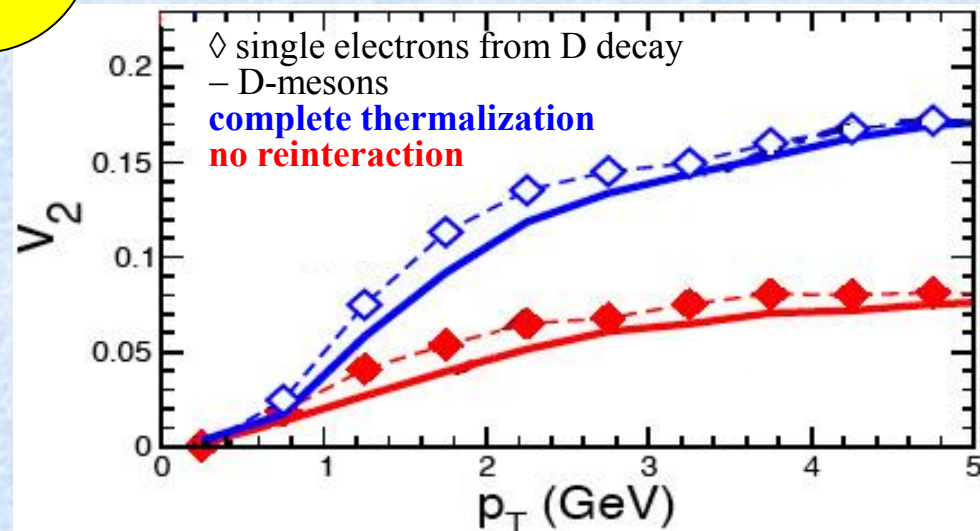
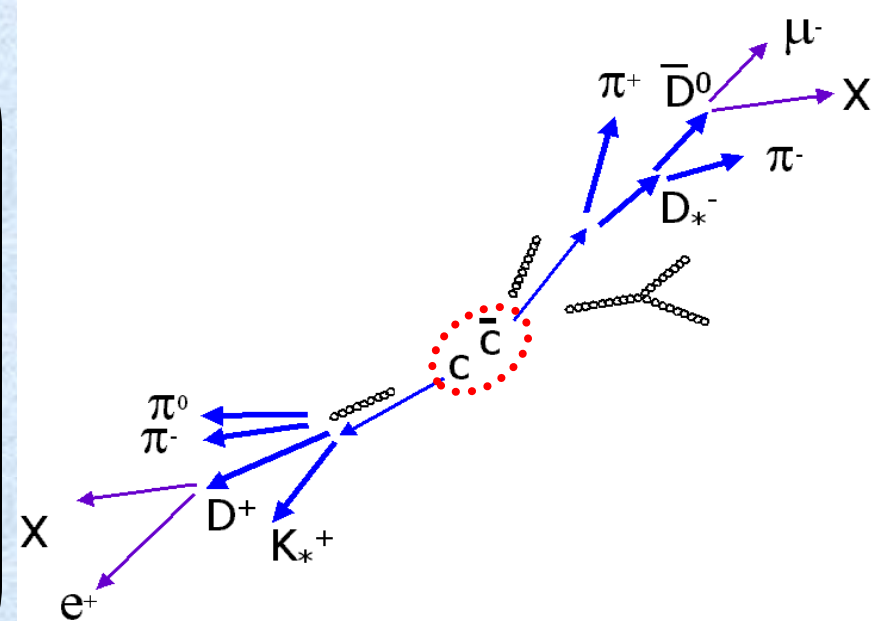
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ground

Heavy flavor electron v_2 :

Is the single electron v_2 representative
of the v_2 of the parent heavy meson?



Possible Scenarios

1. After production heavy quarks do not interact with the medium and eventually fragment in the vacuum

$$v_2 = 0$$

2. Heavy quarks suffer in-medium energy loss before fragmenting, but do not flow

$$v_2 \neq 0$$

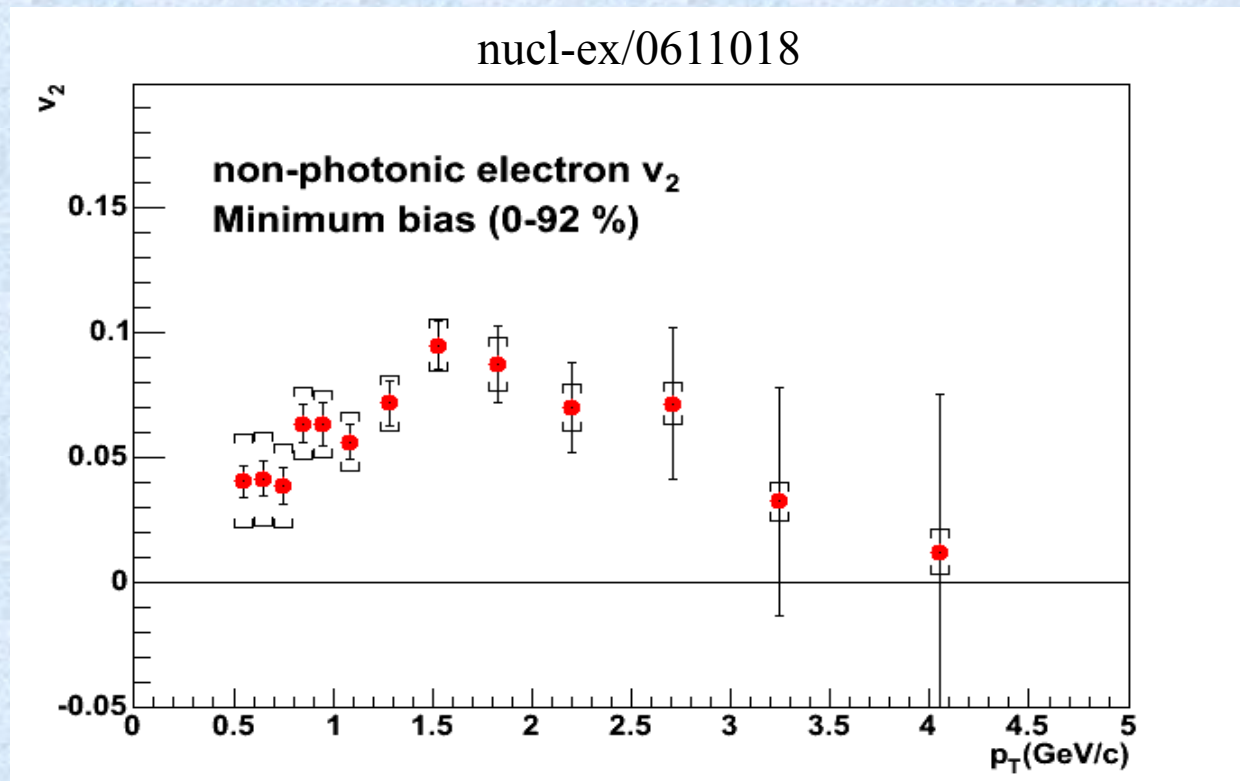
3. Heavy quarks flow in the medium and hadronize via coalescence or recombination

$$v_2 \neq 0$$

4. Heavy quarks do not flow with the medium, but hadronize via recombination and pick up v_2 of light quark partner

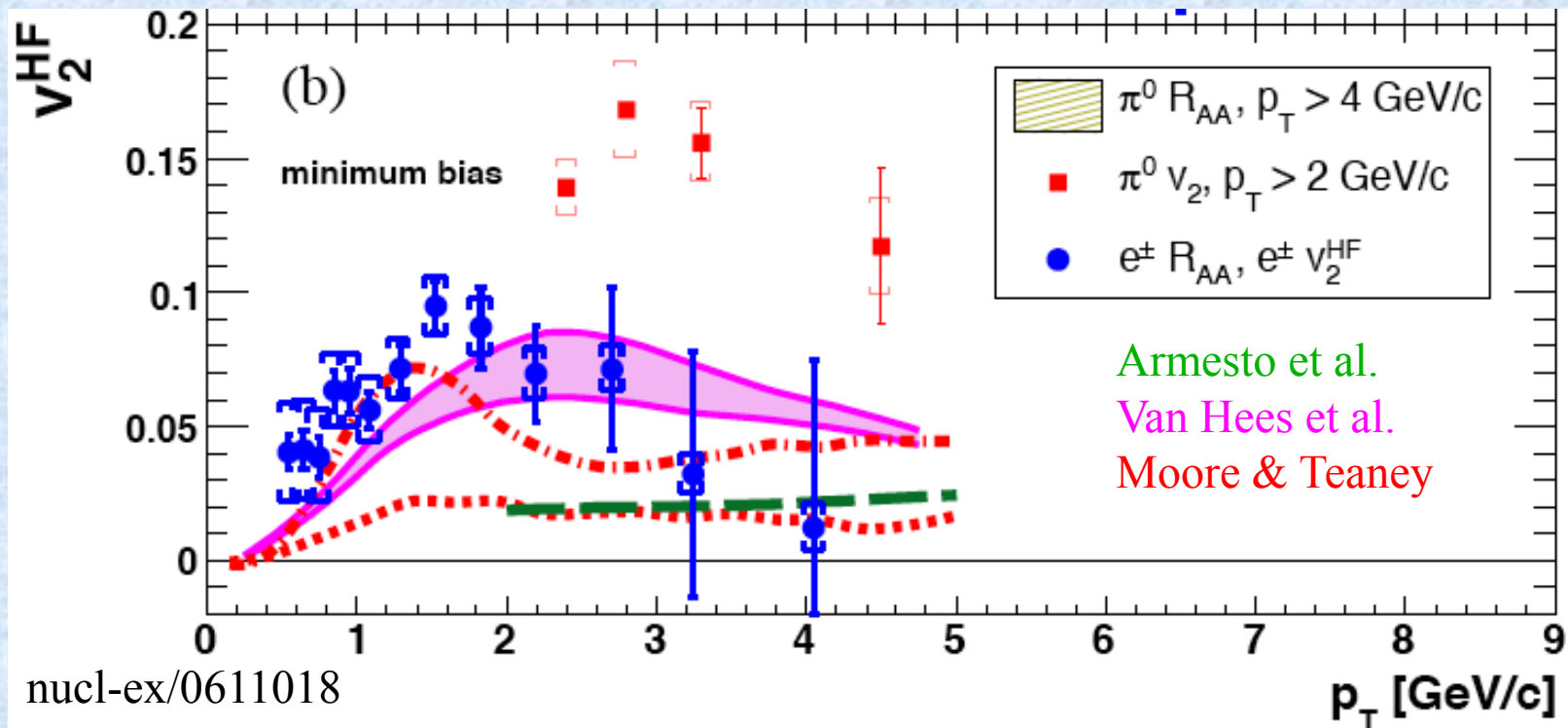
$$v_2 \neq 0$$

Do heavy quarks flow?



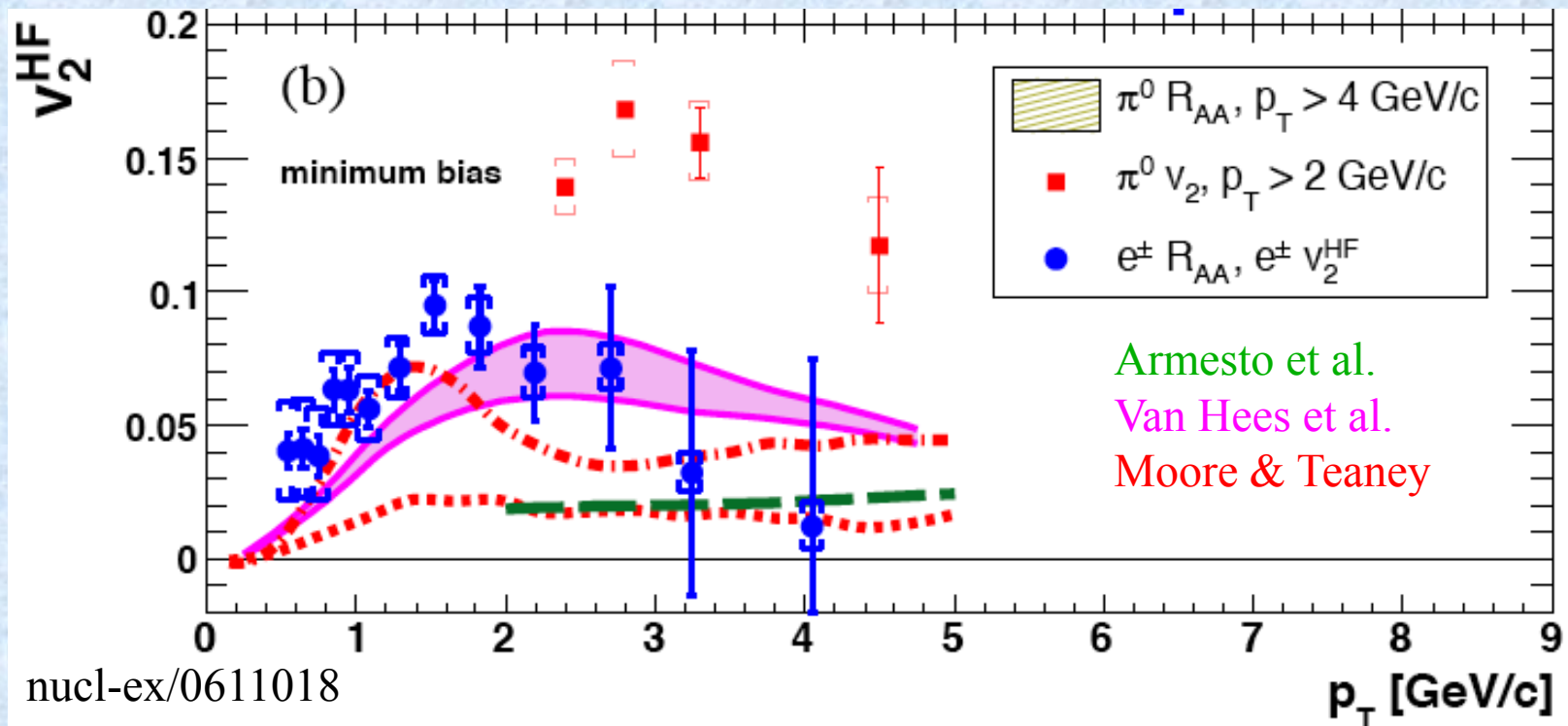
- Sizeable v_2 seen for non-photonic electrons
- Main source of non-photonic electrons (below 2 GeV/c) is D-mesons
- Implies the heavy flavor v_2 is non-zero
- Scenarios 2-4 still possible candidates

Do heavy quarks flow?



- 👉 Armesto - (scenario 2)
 - pQCD calculations with radiative energy loss and large transport coefficient
 - v_2 results from path length dependence of energy loss
- 👉 Heavy quark transport calculations -
 - Require short relaxation time of heavy quarks
 - Small diffusion coefficient

Do heavy quarks flow?



👉 Armesto - (scenario 2)

- pQCD calculations with radiative energy loss and large transport coefficient
- v_2 results from path length dependence of energy loss

👉 Heavy quark transport calculations -

- Require short relaxation time of heavy quarks
- Small diffusion coefficient

Consistent with small values
of η/s near quantum bound

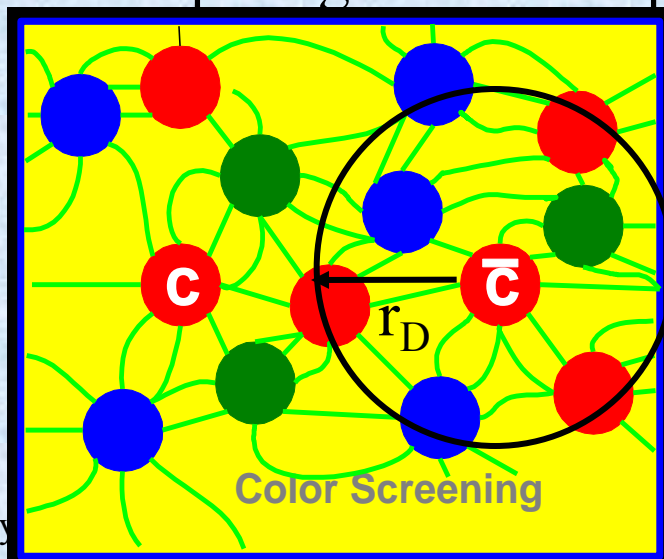
$$\eta/s = 1/4\pi$$

Measurement Limitations

- Scenarios 3&4 still possible:
 - Heavy quarks flow in the medium and hadronize via coalescence or recombination
 - Heavy quarks do not flow with the medium, but hadronize via recombination and pick up v_2 of light quark partner
- Discriminating power of measurement limited by large errors
- Poor statistics at high p_T
 - Region is particularly interesting because it allows access to b-quark through the decay of the B-mesons
 - v_2 of b-quark expected to be small due to large mass
- Improved reaction plane resolution will reduce errors!

Quarkonia

- Quarkonia are of particular interest because....
 - Large mass ($J/\psi = 3096.99 \pm 0.04$ MeV, $Y = 9460.37 \pm 0.21$ MeV)
 - Produced during initial stage partonic collisions
 - Medium interactions convey information about the collision environment
 - Measurements of elliptic flow can probe the degree of thermalization of the medium
- In heavy ion collisions only J/ψ is accessible in PHENIX
- Competing effects are predicted to govern J/ψ production



J/ψ color screening

J/ψ recombination

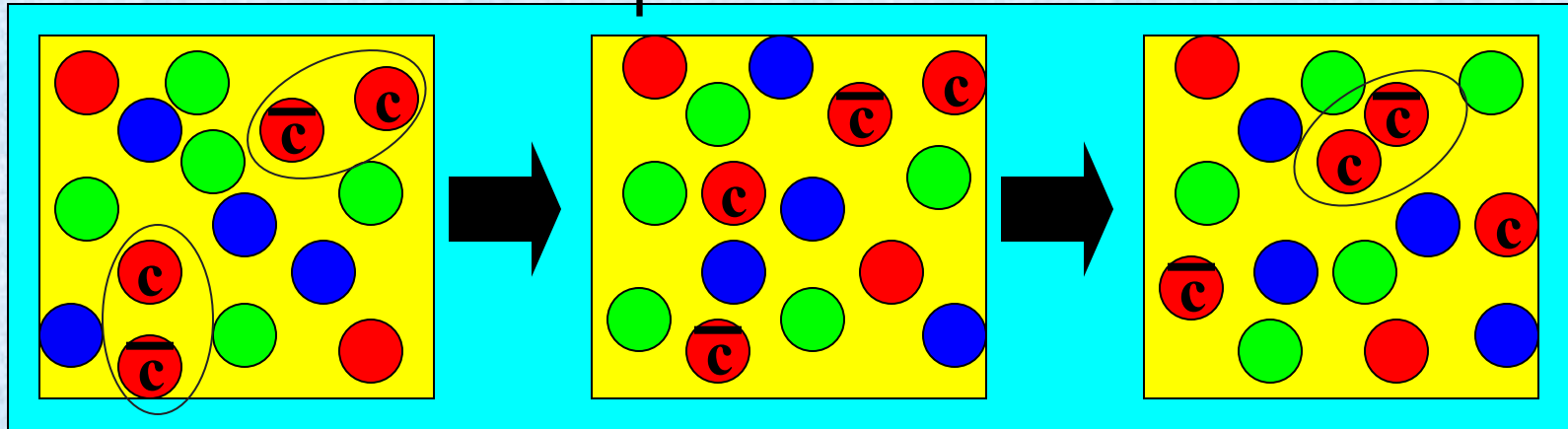
Shadowing

Heavy quark energy loss

Normal nuclear absorption

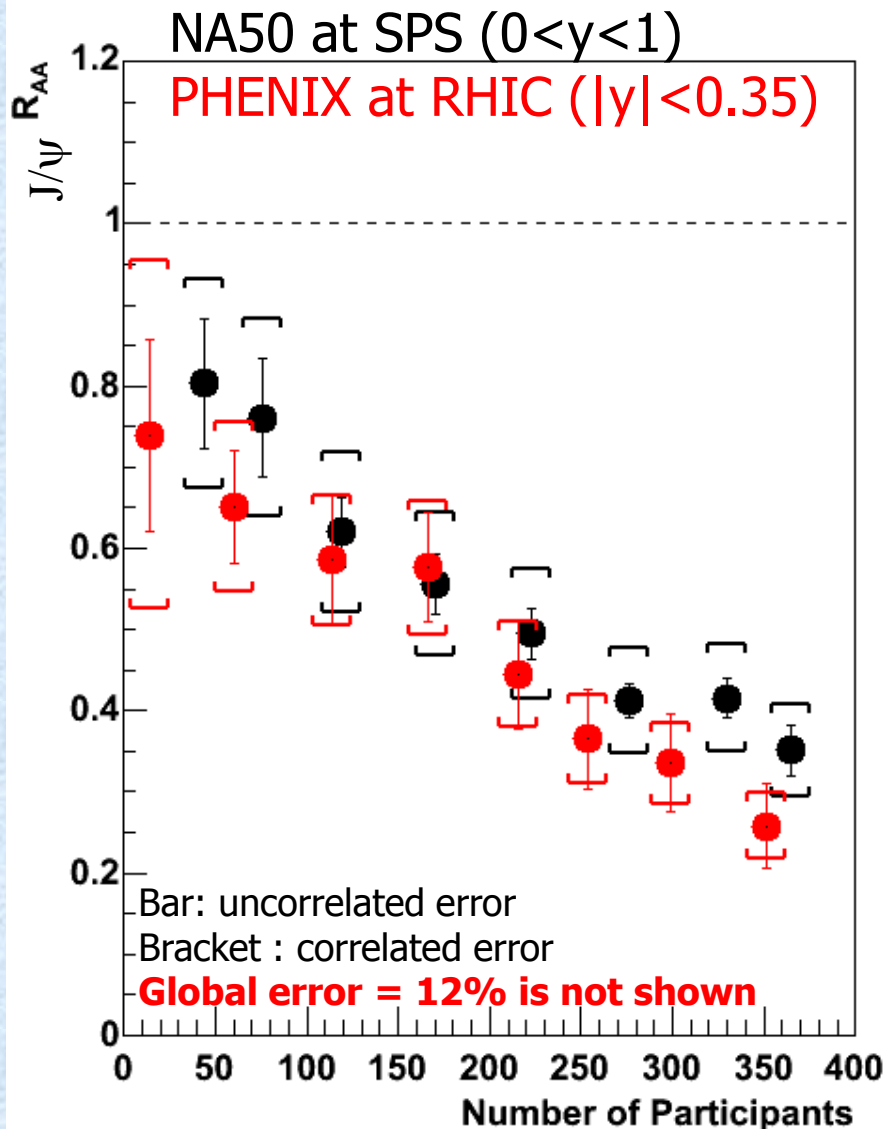
Etc.....

J/ψ Models



- Suppression Models:
 - Assume heavy quarkonia are formed only during the initial hard collisions
 - Subsequent interactions only result in additional loss of yield
 - Suppression of J/ψ yield with increasing collision centrality
- Recombination Models: $c + \bar{c} \leftrightarrow J/\psi + g$
 - In central RHIC heavy ion collisions $\sim 10\text{-}40$ c-cbar pairs are formed
 - Regeneration of J/ψ possible from independently produced c and cbars
 - Leads to an enhancement of J/ψ yield (or less dramatic suppression)
 - Increased J/ψ yield with increasing collision centrality
 - Narrowed J/ψ rapidity and p_T distributions with increasing centrality

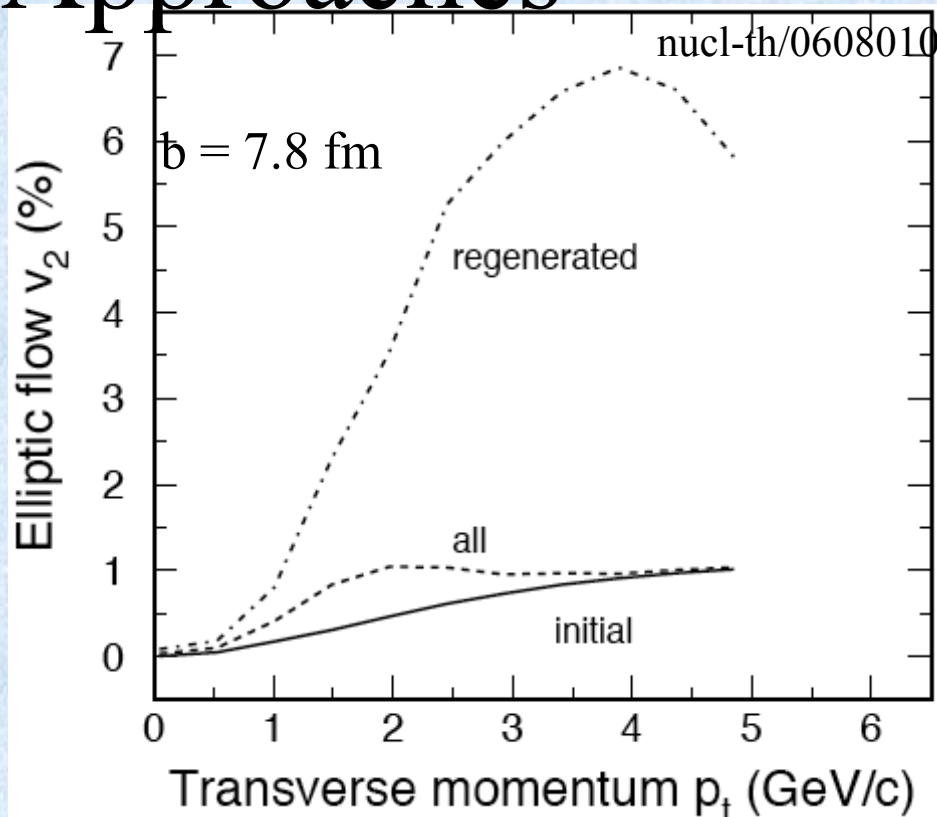
R_{AA} Results



- PHENIX mid-rapidity results show same degree of suppression as observed at the SPS
- Suppression models predict much larger degree of suppression at RHIC energies
- What is the cause:
 - Recombination?
 - Sequential melting?
- J/ψ v_2 can help to distinguish between models

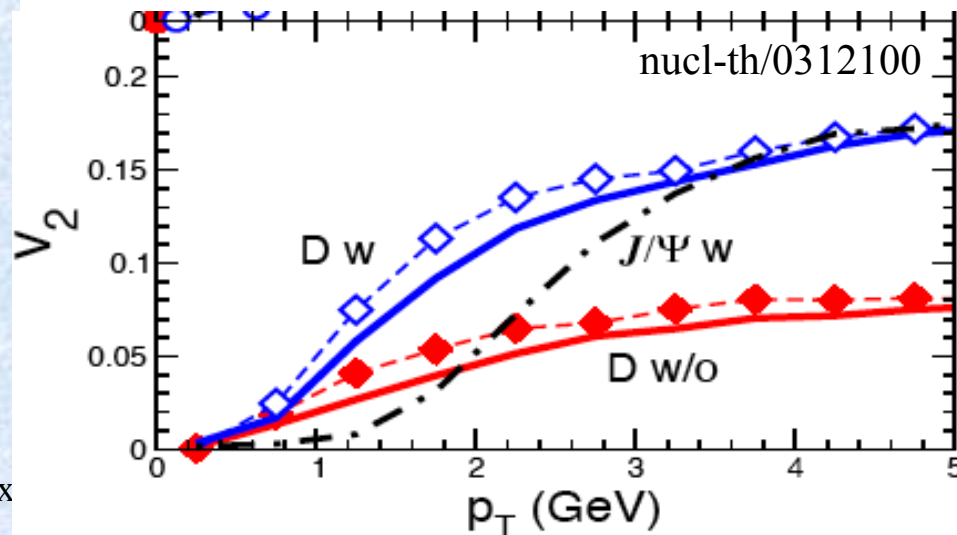
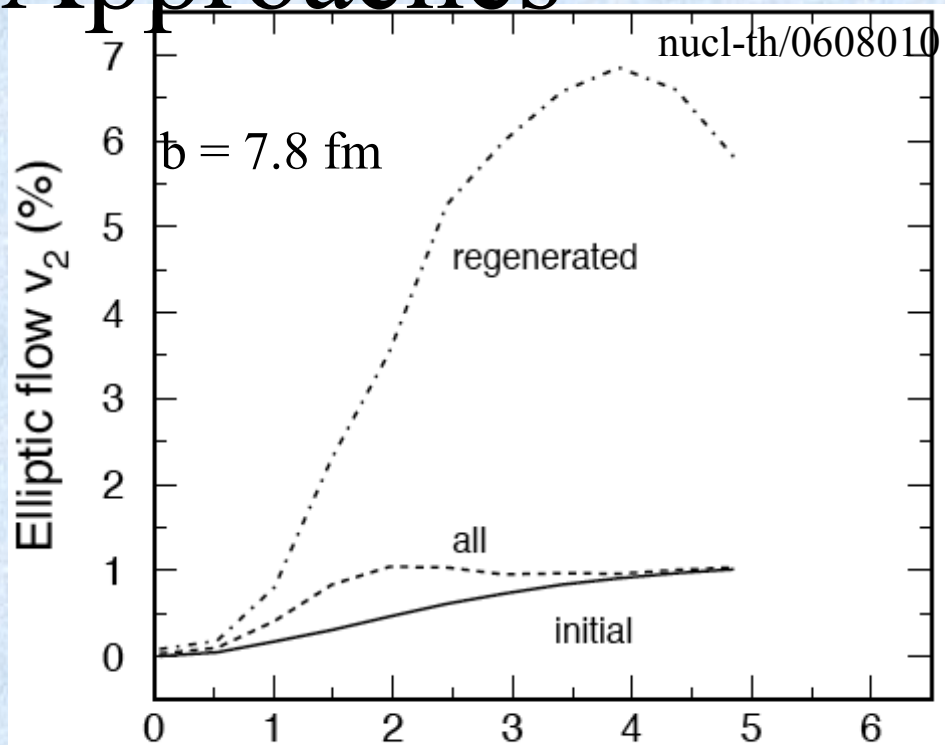
Theoretical Approaches

- Continuous regeneration in collision volume:
 - Weak interaction limit:
 - Charm quarks retain original momentum & spatial distribution
 - No in-medium interaction results in no v_2
 - Strong correlation to medium:
 - Charm quarks thermalized and spatially statistically distributed
 - J/ψ yield still dominated by initial production
 - Small average v_2



Theoretical Approaches

- **Continuous regeneration in collision volume:**
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 - Strong correlation to medium:
 - Charm quarks thermalized and spatially statistically distributed
 - J/ψ yield still dominated by initial production
 - Small average v_2
- **Regeneration at hadronization:**
 - Charm quarks experience complete thermalization
 - No contribution from initially produced J/ψ
 - Large v_2



Do quarkonia flow?

What have we been able to measure so far....

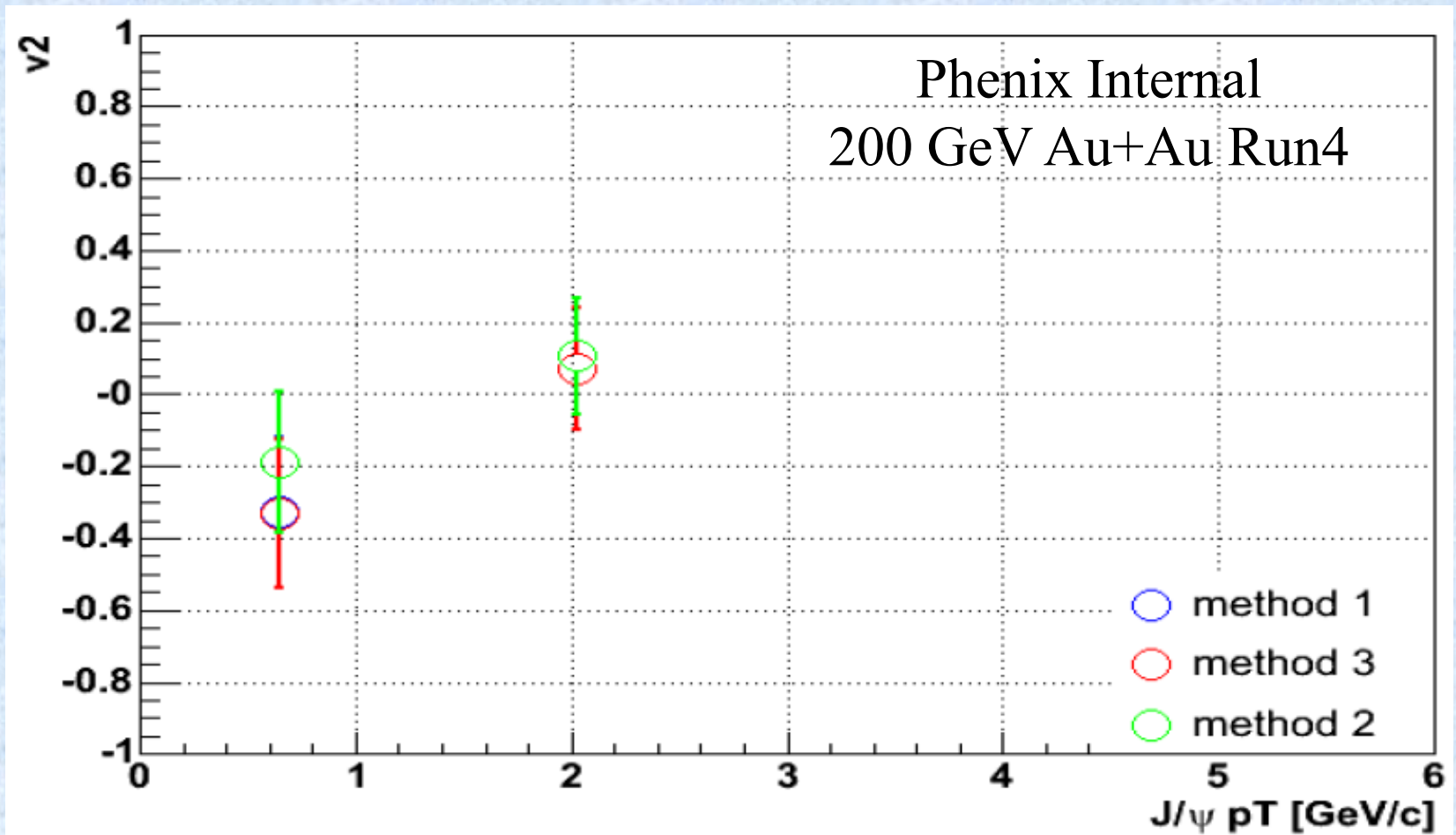
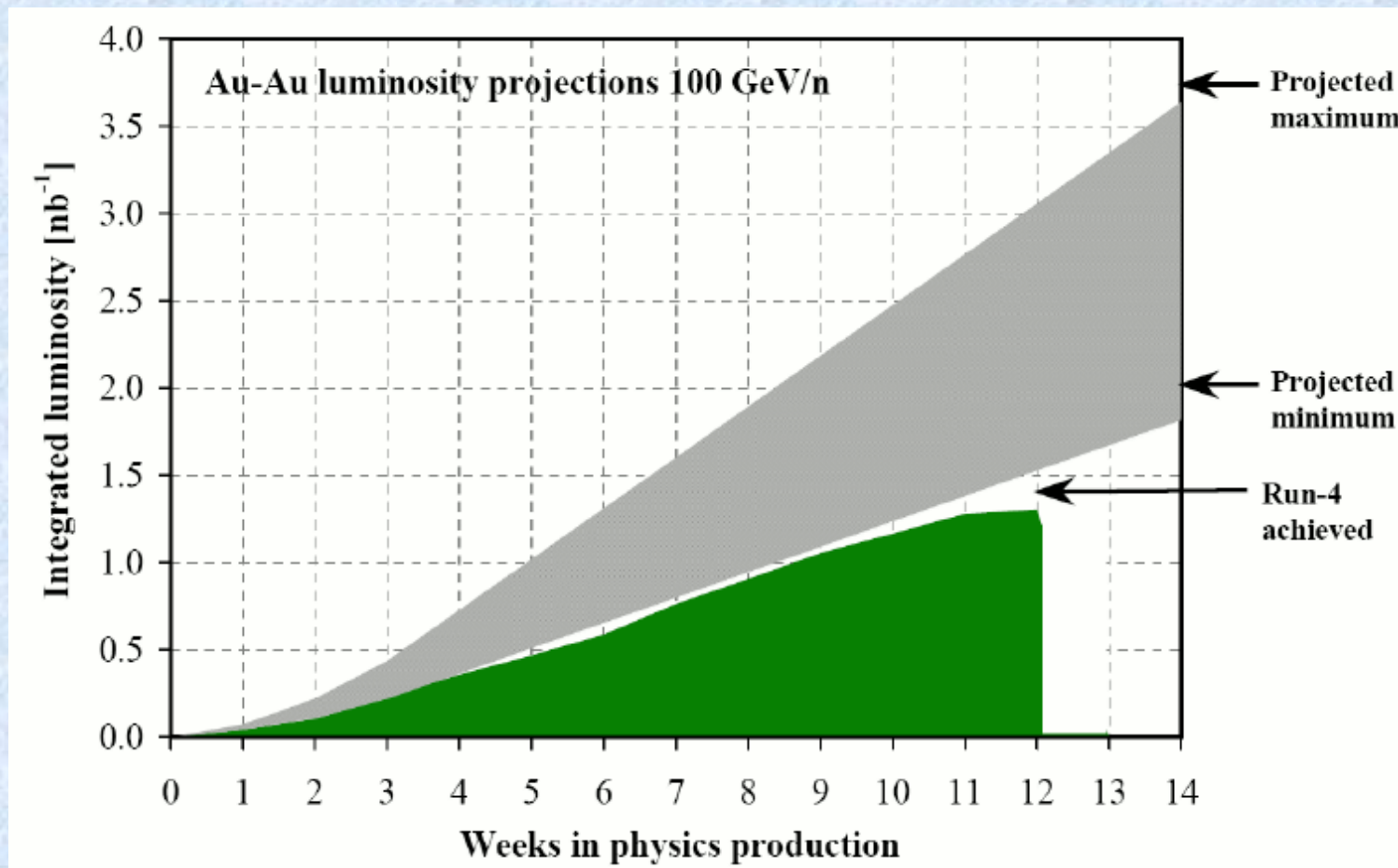


Figure 1.3: The v_2 of J/ψ in minimum bias Au+Au collisions.

Run 7 Prospects



- Based on CAD projections for machine performance

Run 7 Prospects

Run Length (wks)	Mean Luminosity Delivered (nb ⁻¹)	PHENIX Luminosity (nb ⁻¹)	PHENIX Events (x10 ⁹)
14	2.56	1.15	7.3
12	2.16	0.97	6.1
10	1.71	0.77	4.9
8	1.29	0.58	3.7
6	0.92	0.41	2.6
4	0.51	0.23	1.5
2	0.17	0.08	0.5

Run4
equiv

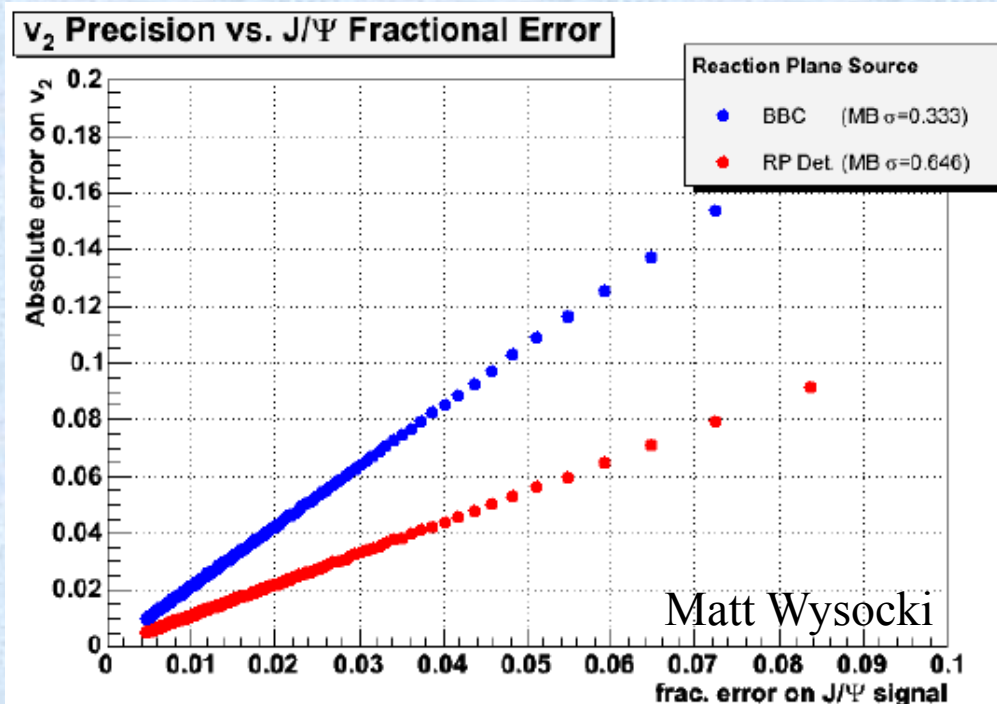
- Calculations presented at H/L by Tony Frawley
- Assumes PHENIX efficiency factor of 0.45 =
Up time(70%) * vertex cut loss(80%) * daq dead time (80%)

Run 7 Prospects

- Lets assume we get 14 weeks 200 GeV Au+Au physics:
 - Equivalent to x5 in events
 - Run 4 dimuon $J/\psi \sim 4500 \Rightarrow 22500$
 - Run 4 dielectron $J/\psi \sim 1000 \Rightarrow 5000$
- What magnitude of statistical error could we expect on a J/ψ v_2 measurement?

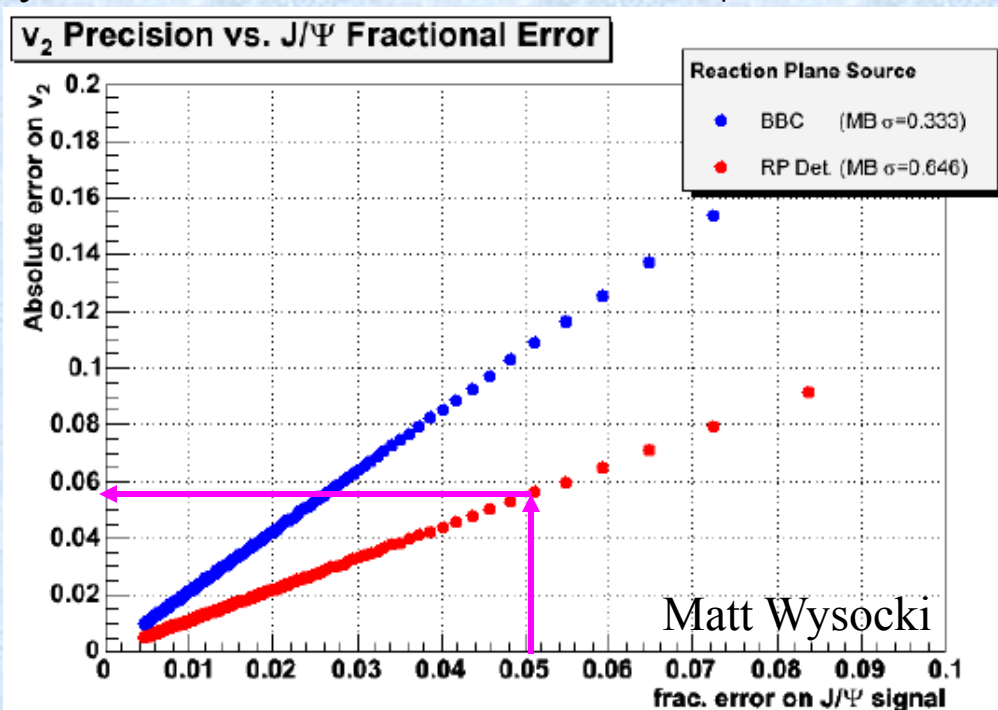
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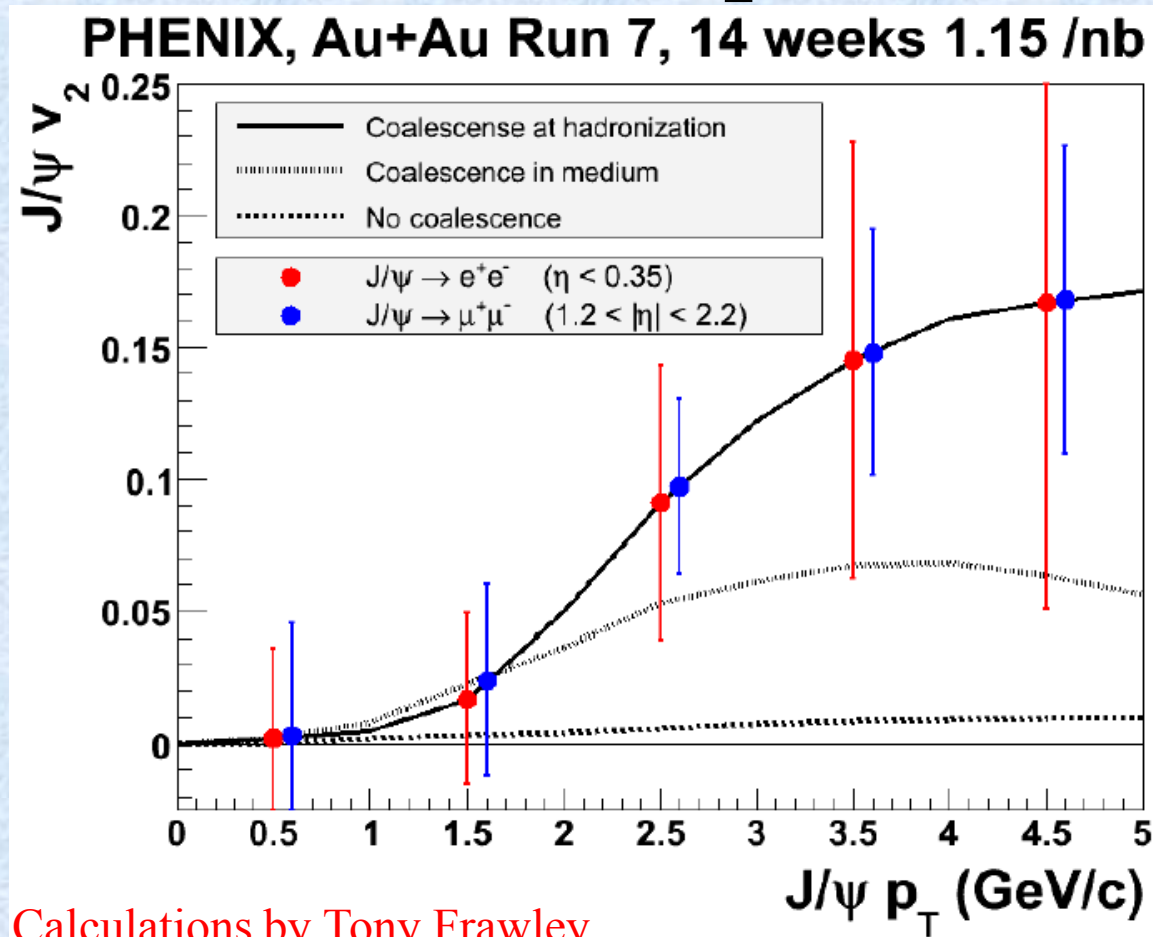


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Run 7 Prospects

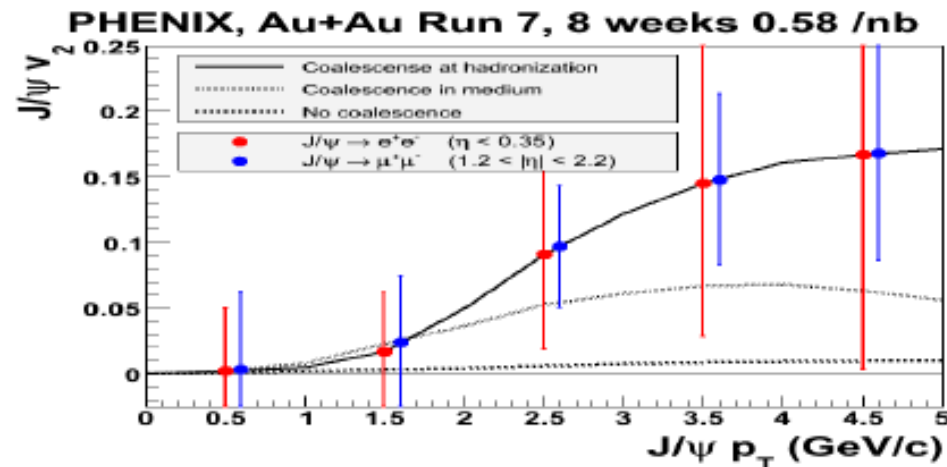
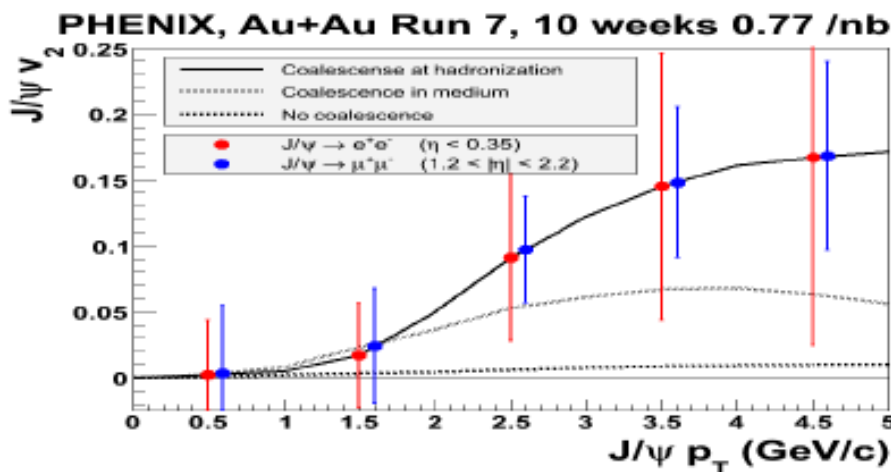
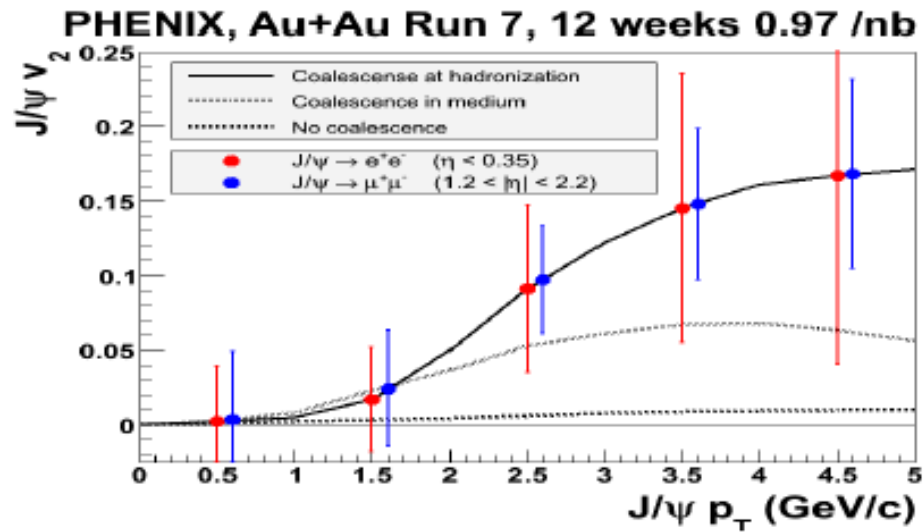
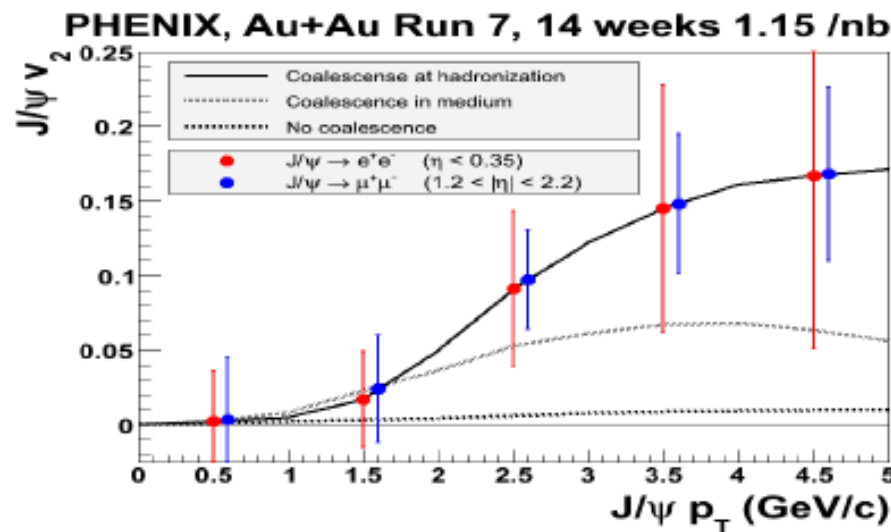


Calculations by Tony Frawley

- Statistical error bars indicate expected discriminating power of measurement
- Curves demonstrate range in available model parameterizations
- Point positions are arbitrary => key is errors

Run Length Dependence

Calculations by Tony Frawley



Questions & Answers

1. What does the reaction plane detector actually measure?

- Resulting signal is proportional to the original energy deposition in each individual segment
- Increased energy deposition occurs in those segments aligned with the reaction plane
- Allows event-by-event determination of reaction plane

2. How is this incorporated into physics analyses?

- Flow variables measured wrt reaction plane
- Resolution must be applied as a correction factor to any measurement of flow

3. What do these measurements tell us about the collision medium?

- Thermal equilibration occurs on short timescales
- Matter is a strongly interacting partonic medium
- Future studies will shed light on:
 - Heavy flavor in medium behavior and production/regeneration mechanisms
 - Parton energy loss as a function of path length in the medium from high p_T π^0 's
 - Test predictions of jet-medium interaction as a function of path length in the medium with intermediate p_T direct photons

Dependence of v_2 error on v_2 of J/ψ and Background

Measured v_2 error vs. input J/ψ v_2 and bgnd v_2

